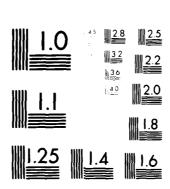
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PIPING INELASTIC FRACTURE MECHANICS ANALYSIS

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LWR pipe rupture Tearing modulus

LWR pipe rupture Fracture toughness

Crack opening angle

Leak-before-break

Pseudo toughness theory Flow stress theory

J-resistance Stability index

J-controlled crack growth

Energy release (or dissipation) rate

20. ABSTRACT (Continue on reverse side if necessary and identify by block number)

Available experimental data and the analytical methods for predicting rupture of LWR piping are assembled and assessed. The analytical techniques investigated can be catologued into three major groups: structural response, semiempirical methods, and the J-controlled growth approach. A leak-before-break condition is also investigated.

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PIPING INELASTIC FRACTURE MECHANICS ANALYSIS

1.0 SUMMARY

This report summarizes the results and conclusions of Task 1 and 2 of the study on "Piping Inelastic Fracture Mechanics Analysis", Contract Number (NRC-03-79-116). In these tasks, available experimental data and the analytical methods for predicting rupture of LWR piping have been assembled and assessed. The analytical techniques investigated can be catalogued into three major groups. These are gross structural response analysis, semiempirical methods, and the J-controlled growth approach.

The gross structural response is computed using numerical techniques when dynamic behavior of both the piping and the fluid is considered. The LWR piping stability is modeled by allowing a preassigned crack to propagate under a certain toughness criterion such as K_{Ic} , K_{Id} or maximum strain at the crack tips. In this analysis, the accuracy of the results depends very heavily on the crack growth criterion about which little information is known. When brittle failure is observed, K_{Ic} or K_{Id} may be adequate. For a pipe that fails plastically or in a mixed brittle/ductile failure mode, well established fracture criteria are not yet available. In addition, a single computer run frequently provides numerical results which may not be extrapolated to other cases where computing costs prevent additional runs to be made.

Depending upon the piping materials and their service temperature, a semiempirical approach has been proposed to study elastic/plastic fracture of LWR piping. A pseudo-toughness parameter, K_c , has been derived from classical fracture mechanics theory and modified to describe the toughness of the piping made of low to medium toughness materials. Unfortunately, poor correlation was found between the pseudo-toughness, K_c , and experimental results. For high-toughness materials, a flow Manuscript submitted April 30, 1980.

stress theory has been proposed. In this case, the theory characterizes the piping stability by its 'imit load carrying capability and contains no fracture parameter of any type. By properly adjusting the flow stress value, experimental results from tests on piping made of high toughness materials suggest that the flow stress theory may be adequate. However, upon further evaluation, it is revealed that structural stability is influenced by both crack tip conditions as well as structural geometry. Therefore, more conclusive analytical or experimental evidence is needed before any conclusion can be drawn regarding the adequacy and the applicability of the semiempirical methods in LWR rupture prediction.

One of the most promising and most rigorous predictive methods to date is the J-control growth. J_{Ic} has been accepted as an elastic/plastic fracture initiation criterion and the existence of a HRR (Hutchinson-Rice-Rosengren) field has been identified as the necessary condition of a J-dominated stress field. Once a crack starts to propagate, however, large deformations and unloading near the crack tip region are expected; these factors are not accounted for in the original J-theory formation where infinitesimal deformation and deformation theory of plasticity (no unloading) are assumed. Nevertheless, extensive research effort has been directed to extend J to a governing crack propagation criterion in spite of its underlying assumptions. Other crack extension criteria, closely associated with the J-controlled growth, include crack opening angle (COA), tearing modulus (T), finite stretch and stability index (λ_I). It is noted that these extension criteria are all related and permissible in treating a limited amount of crack growth.

A leak before break condition is expected for high toughness materials as well as medium to high toughness materials at shelf temperature. The large critical flaw sizes associated with these materials suggest that extensive leaking, as well as general yielding, will precede attainment of a critical fracture condition. There are simplified methods to compute mouth opening for pipes of these materials in transition region; however, their accuracy remains to be established.

2.0 INTRODUCTION

The purpose of this work is to study nuclear reactor pipe failure due to elastic/plastic fracture. The scope of this study includes definition of critical flaw size-stress level conditions necessary to induce structural instability. Subcritical growth mechanisms, such as fatigue and stress-corrosion, as well as crack arrest will not be discussed. A primary objective here is to assemble and to ultilize existing experimental data and analytical tools toward the study of elastic/plastic pipe rupture. Therefore, no basic research in the fundamentals of elastic/plastic fracture mechanics or experiments in generating new data are included. Only limited amount of information is included for the analytical methods presented in this report. Details of the formulation and justification should be referred to the original work which are included in the references. In this report, vast amount of experimental data has been collected for later use; but details of experimental techniques and variables are partially omitted.

2.1 LWR Cracking Experience

Cracking of LWR piping was first observed Dec. 1965, when a leakage was found in a 6 in. bypass line of the recirculation loop in Dresden I. Between 1965 and 1975, cracks were discovered on many 4 in. diameter 304 s.s. pipes for recirculation loop valve bypass, and on 10 in. diameter 304 s.s. reactor core spray lines (Figs. 1 and 2) in six domestic Boiling Water Reactors. These BWRs are Dresden 2, Quad City 1 and 2, Millstation 1, Peach Bottom 3 and Monticello. Subsequent investigation [1] has concluded these flaws were produced by intergranular stress corrosion cracking (IGSCC) and are due to the combined effects of stress, oxidization, sensitization and fatigue growth. Subsequent to 1975, IGSCC has also been found in other location such as reactor-water-clean up lines and control-rod-drive-return lines. In 1978, cracks in large diameter pipes (greater than 20 in O.D) were discovered. In this case, extensive cracking was found on a 24 in. diameter recirculation-inlet-nozzle safe end (Fig. 3) at the Duane Arnold Plant. Following intensive investigation, NRC's pipe crack study group [2]

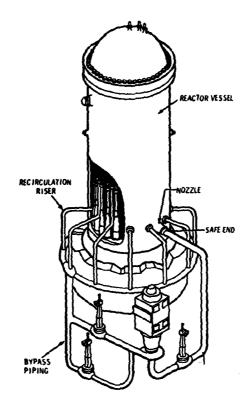


Fig. 1-BWR Recirculation System

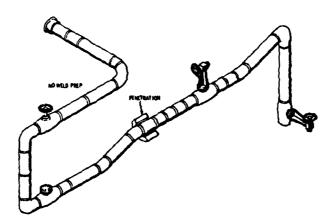


Fig. 2-Dresden-2 core spray-loop A (north)

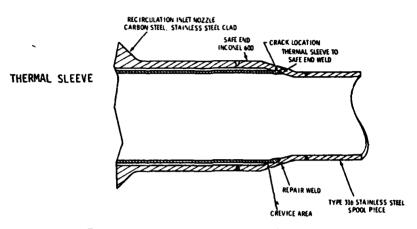


Fig. 3.1-Duane Arnold recirculation-inlet-nozzle safe end configuration

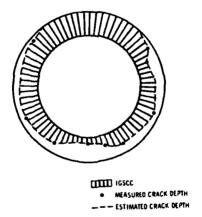


Fig. 3.2—Representation of IGSCC in Duane Arnold leaking recirculation-inlet-Nozzle safe end

concluded that the crevice geometry at this location and the sensitized material enhanced the IGSCC mechanism even on these larger pipes.

The stress corrosion problem in PWR is not as severe as that in BWR due to low oxygen content in the water and fewer furnace-sensitized safe ends. Therefore, no problem has been experienced in PWR primary systems. Nevertheless, in the secondary system, inter and transgranular stress corrosion cracking has been observed in these locations where relatively stagnant boric acid solution are present.

The impurities were introduced by safety injection and borated water make-up systems. At Arkansas 1, Ginna and Surry 1 plants, the piping involved were Type 304 s.s. in 8 in. and 10 in. sizes.

A detail complication of the LWR failure experience can be found in References 3 and 4.

2.2 Materials, Geometry and Environment

The most commonly used materials in the LWR piping system are Types 304 and 316 austenitic stainless steel (cast/wrought). However, for various reasons, such as intergranular stress corrosion prevention or others, ferrific steels such as SA-333, SA-106 and SA-516 have also been used. Feed water lines in PWR and steam lines in BWR are typical examples. Table 1 is a comparison of the tensile properties of these materials. In addition, low carbon stainless steel 304L or 306L and other stress corrosion resistant materials have been recommended for piping applications [1].

The piping system in LWR is very complex and a typical 4-loop Westinghouse configuration is shown in Fig. 4 [2]. It can be classified by its functional requirements or by the material, geometry and environment to which it is subjected. In this report, since only the consequence of the existence of a flaw is to be investigated, a pipe is referred by its size, material composition, and the loading on it. At this point, it should be noted that nearly all the cracks discovered to date are located in the weldment or HAZ where the piping is connected to the nozzle. These connections may be to the reactor vessel, steam generator, feedwater system pressurizer, or other components. Although the major loads on the system are pressure, thermal and mechanical loads (e.g. seismic and water hammering), the contribution of the residual stress due to the welding plays a very important role in initiation and propagation characteristics of cracks. If pressure stress dictates the pipe failure, only axial cracks resulting from large hoop stress are possible. However, the combined effects of material sensitization, residual stress

TABLE 1. Material Tensile Properties of Ferritic Steels

Tensile	63		0
	$\frac{8}{100}$		70 70–90 35
	2 65 35	20 40 40	65 5-85 35
	4 6 7 50 60 65 35 35 35	V 4	65 -
	_ , ,	B 60 35	60)-80 32
	35 35		. 09
	$\frac{1}{55}$	A 48	55 60 65 55-75 60-80 65-85 30 32 35
	Grade $\sigma_{\mathbf{u}}$	$\begin{matrix} \sigma \\ \sigma \\ \sigma \\ \sigma \\ y \end{matrix}$	Grade o o y
Impact Requirement	Yes!	No!	Improved notch toughness
Material	A-333 (Seamless and Welded steel pipe for low temperature service)	A-106 (Seamless carbon steel pipe for high temperature service- 1/8 to 26 inches)	A-516 (pressure vessel plates, carbon steel, for moderate and low temperature service)

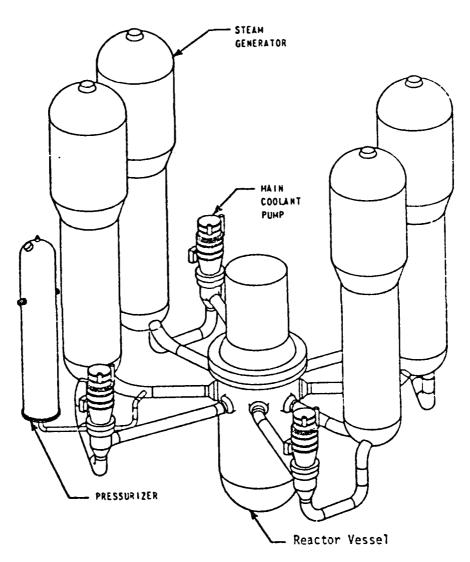


Fig. 4— Primary pressure boundary of a typical 4-loop Westinghouse Nuclear Power Plant

from welding processes, pressure and bending stress often initiate and propagate cracks in the circumferential directions. In addition, because both bending and residual stresses are self-equilibrating quantities, failure generally initiates at the surface where the combined stress is the largest. In the study of pipe integrity, both surface and through-wall cracks are of equal importance.

The operating conditions of a typical Pressure Water Reactor (PWR) is at a pressure of 2235 psi and at temperature of 650°F. The Boiling Water Reactor (BWR) is operated at around 1035 psi and 550°F. The size of these pipes are approximately 30 in. diameter for main loop and steam generator loop, and 6 to 14 in. diameter for the other large branches.

2.3 Material Characteristics and Fracture Toughness

Toughness is one of the material properties that is essential to the integrity of a structure. The actual material toughness is both geometry dependent and temperature sensitive. Because of the microstructural variation and different constraint condition surrounding a sharp flaw, a component can have brittle failure, ductile rupture or mixture of both.

To illustrate this phenomeon, a schematic Dynamic Tearing (DT) test result of fixed thickness specimens are shown in Fig. 5. At the Nil Ductility Transition (NDT) temperature, the fracture is brittle and shows a flat, featureless surface. A rapid increase in fracture energy is recorded at temperatures above NDT as more ductility is developed which is evidenced by increase in lateral contraction and development of shear lips. As the temperature exceeds shelf temperature, brittle cleavage appearance is replaced by ductile dimple type failure and there is no further increase in fracture resistance above this point. The basics of this fracture energy/temperature relationship can be explained from the differences in microstructural failure modes. Brittle failure at temperatures considerably below the shelf involves pure cleavage of the individual grains and is a high-speed process. However, upon increasing

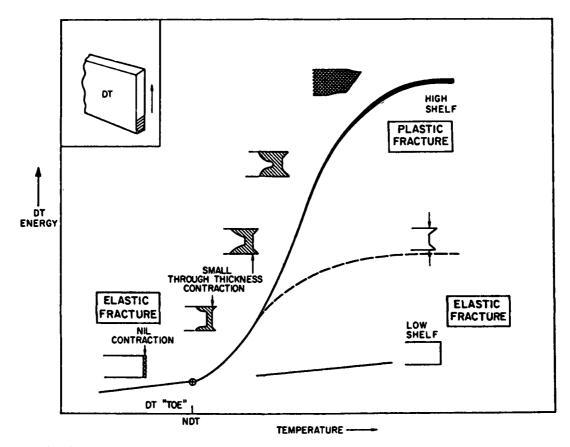


Fig. 5—DT test transitions to various levels of shelf fracture toughness. Note that with a decrease in shelf level fracture energy there is a corresponding change from fractures with large lateral contraction to flat fractures with nil contraction features. The decrease in shelf energy marks a transition from plastic (plane stress) to elastic (plane strain) fracture conditions.

in temperature, cleavage separation of individual grains competes with slip processes. More energy is required for attaining higher stress needed for cleavage because more strain is required for elevating flow stress to the level of the cleavage stress. Macroscopically, in the transition region, the increase in fracture toughness is accompanied by the development of shear lips at the fracture surface. Finally, at the upper shelf temperature, fracture process is defined by microvoid coalescence; when small voids between grains, or of inclusions or impurities, are opened and the metal bridges between these voids

are stretched as tiny tensile specimens which finally rupture in a progressive ductile mode. The transition temperature and the sharpness of transition region depends on the specimen thickness (Fig. 6). Generally, the thinner specimen exhibits lower transition temperatures.

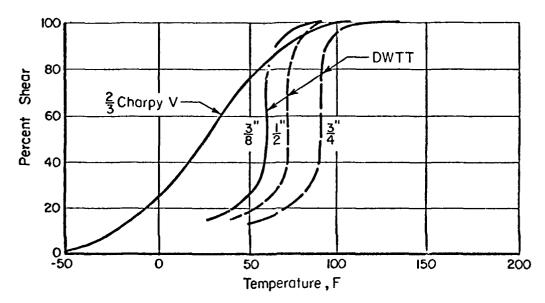


Fig. 6-Effect of plate thickness on DWTT and Charpy shear area results

The validity of linear elastic fracture mechanics (LEFM) is limited to small scale yielding. When the size of plastic zone developed in the specimen exceeds a prescribed limit (Fig. 7) due to changes in service loading or increase in temperature, K_{Ic} [6] or K_{Id} looses its usefulness. The region of valid LEFM toughness determination is restricted to the temperature (T) and energy level (S) limits indicated in Fig. 8. Fortunately, the J-integral [7-16] approach has extended the material toughness measurement to upper shelf region. The development of J-integral concept and testing technique not only has reduced K testing effort by using smaller specimens but also has enabled structural engineers to characterize a flawed body subjected to large scale yielding. However, the validity of J-integral approach is limited theoretically due to its basic assumptions [7] such as infinitesimal deformation, deformation theory of plasticity etc.

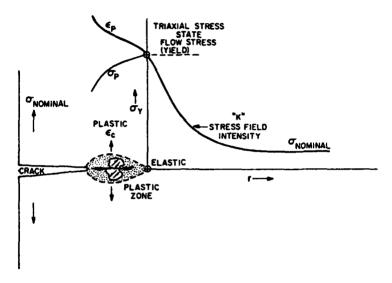


Fig. 7—Relationships of elastic and plastic stress fields to the plastic zone at crack tips for the case of plane strain constraint. As plastic relaxation is developed (large plastic zone and crack tip blunting), the elastic stress fields are replaced by plastic strain fields. Elastic stress field K definitions are not possible for these conditions.

Under normal reactor operating conditions, materials that have been used for nuclear piping construction can be identified as those exhibiting no transition temperature and those having a definite transition temperature. Austenitic stainless steel, 304 and 316 s.s., are examples of the first kind and ferritic steels are the second type. Therefore, austenitic stainless steels are materials having very high toughness and the structural failure is generally related to limit load conditions. Figure 9 illustrates the J-R curves of 304 and 316 s.s. at room temperature as well as 600° F [17]. The J_{lc} (critical initiation value) ranges from 5000 in. lb/in.² at RT to 3500 in. lb/in.² at 600° F. Using the K_{lc} - J_{lc} relationship:

$$K_{lc}^2 = \frac{EJ_{lc}}{1 - \nu^2}$$

where E is the modulus and ν is Poisson's ratio, the critical stress intensity factors K_{lc} are 375 ksi $\sqrt{\text{in.}}$ and 300 ksi $\sqrt{\text{in.}}$, respectively. With such high toughness values, it is obvious that these materials have high tolerance against brittle fracture, and the structural failure must be controlled by ductile tearing.

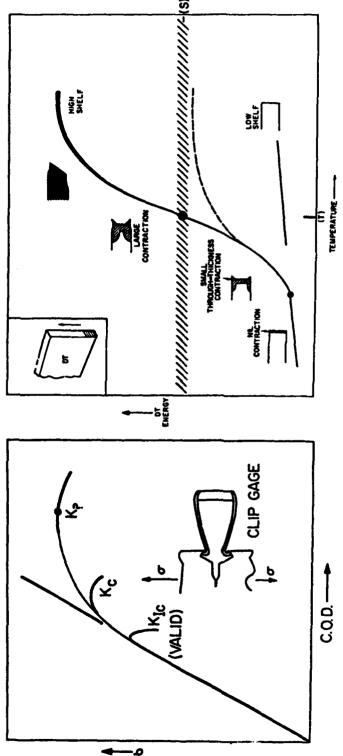
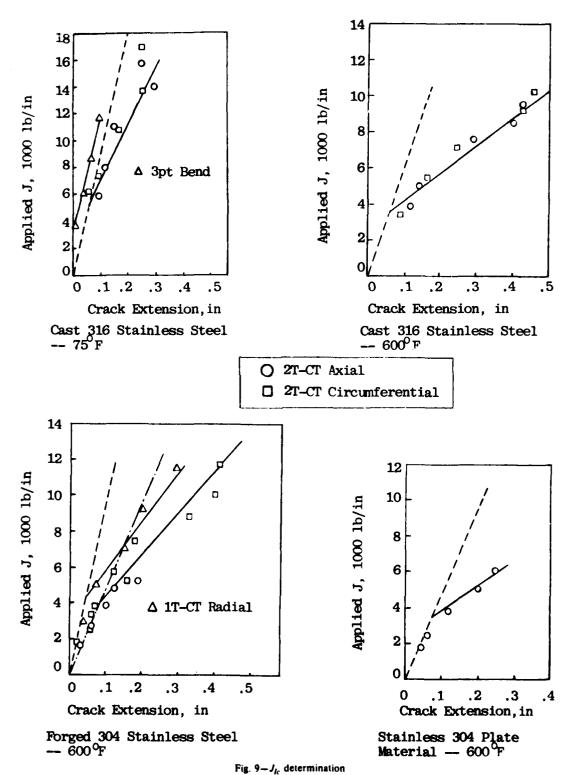


Fig. 8—Relationships of Crack Opening Displacement (COD) features of K_{lc} test specimens to DT energy transition curves featuring highand low-shelf characteristics. Valid K_{Ic} values involving clastic COD instability can be attained only to temperature (T) and shelf (S) limits of the DT test which involve small amounts of lateral contraction. Fractures of DT test specimens involving plastic deformation document plane tress conditions (R, or R).



When attention is directed to the materials of second type which have lower toughness and exhibit a definite transition temperature, the structure failure is no longer controlled by ductile tearing alone. Depending on the operating temperature regime of the material and the geometry of the structure (thickness, pipe size and surface flaw or through-wall flaw), brittle fracture and/or ductile tearing is possible. Generally, the material toughness characterization tests and structural failure analyses of these types of materials are more complicated and less conclusive.

3.0 COMPUTATIONAL METHODS OF NUCLEAR REACTOR PIPE RUPTURE

Typically, the pipe rupture study can be classified as near field or far field study. The terms, near and far, denote the relative size of the region around the crack tip where the analysis is employed. In the far field computational method, a considerable amount of effort is directed to model the overall structural response of piping system, and the crack tip behavior enters into the analysis only as a simple fracture criterion. On the other hand, near field study deals with the materials and structural response locally near the cracked region. The overall structural response affects the local stability only in the compliance formulation.

In the far field computation, the whole piping system is generally modeled by 3-D solid or shell finite elements. The dynamic behavior, produced by an advancing crack, of the piping system and the fluid inside are considered. Because of the computational complexity in dealing with the overall structural dynamics of the piping system, only the simple crack extension criterion can be included in the iterative process without prohibitive computational time. The commonly used criteria are either maximum strain or K_K .

In the LEFM analysis, toughness can be considered as a material property. The stability of a flawed structure is conservatively assured when the applied stress intensity factor is less than the critical

value, K_{IC} . This is the basic philosophy that the ASME boiler and pressure vessel code has adopted. Because the structural stability is measured by a near field parameter K, this type of analysis can be considered as a near field analysis. Another example of the near field approach is the fracture mode transition temperature method, where the operating temperature is used to control structural failure against fracture initiation and propagation of existing flaws. However, when cracks advance into material resulting in large deformation, stability against fracture may depend on material as well as geometry and loading conditions. In this case, better failure description is needed. The J-integral approach is rigorous in defining fracture initiation under gross plastic yielding. Evidence to date indicates that the J-R resistance curve may be useful in studying crack propagation under monotonic loading. If one accepts this assumption, the J-R resistance curve approach can also be considered as a near field analysis method.

Both near field and far field methods assume that the local instability criteria are dependent only on the material. However, the structural geometry and the loading are needed in the structural/material response computation. To make this complicated problem more trackable, much effort has been directed to develop a simple analytical formulation which considers the material properties as well as structural geometry and loading conditions. The technique used in generating these formulations is generally semi-empirical in nature. Starting from a known solution for a flawed plate, modifications to account for plasticity and geometry effects are first incorporated. The final simplified solution is derived by verification and adjustment of the modified formulation using a vast amount of experimental data.

In the next several sections, detailed discussion of each computational method will be presented.

3.1 Gross Structural Response

This type of computational method is far field study because the analysis includes a very large region of the piping system. In addition, the computational emphasis is on the overall response of the structural rather than local region surrounding an existing crack. With improved numerical computation capabilities, pipe rupture can be very easily modeled by finite element or finite difference computer programs. In these analysis, typical shell elements are used to model the piping. Elastic, elastic/plastic, or even viscoelastic constitutive behavior can be employed. In addition, the dynamics of crack opening, coupled with the escape of the internal fluid, can also be included. Depending on the requirement, a very costly program may be developed to model some postulated event. One of the key ingredients in simulating the piping rupture is the requirement of an adequate fracture criterion such as maximum strain or K_{kc} . References 18 & 22 are typical research results of this kind. However, the accuracy of these analytical results depends heavily on a poorly-defined quantity, viz., the fracture toughness of the material. When brittle failure is observed, K_{lc} or K_{ld} may be adequate. For a pipe that fails plastically or in a mixed brittle/ductile failure mode, the analytical prediction can be misleading. In addition, the numerical results of one costly numerical analysis may not be extrapolated to other cases where the prohibitive costs prevent additional runs. The need for this type of analysis is apparent when dynamic fracture (static initiation/dynamic propagation) governs the fracture processes. However, based on the documented nuclear reactor piping field failure experience, there is very little evidence that a pipe failure due to dynamic propagation is likely. The primary reason for a non-propagating crack is the fluid (water) does not enhance dynamic growth in piping. In general, gross structureal analysis is not a very widely accepted method in pipe rupture analysis.

3.2 Semi-Empirical Methods

Before an acceptable inelastic pipe rupture analytical method is developed, the most logical means to study the problem is to rely on known technology. In this case, the existing technology is linear

elastic fracture mechanics. However, one immediately faced with the task of circumventing the inherent limitations built within LEFM. The test specimen thickness requirement is one example. The constraint requirement imposed by ASTM E-399 with respect to determination of the plane strain critical stress intensity factor, K_{Ic} , is

$$B \geqslant 2.5 \left(\frac{K_{lc}}{\sigma_{ys}} \right)^2. \tag{1}$$

For materials having yield strength σ_{ys} , the thickness (B) must be in excess of the actual reactor piping thickness to have an adequate K_{lc} measurement. Since K_{lc} is very sensitive to thickness variation, experimentally generated K_{lc} values can be misleading. Another important consideration in adopting the LEFM approach is extensive plastic yielding during the failure process. If pipe failure is due to gross plastic yielding, the elastically-generated fracture toughness value becomes meaningless.

To account for the LEFM limitations as well as the geometry and loading conditions on a pipe, semi-empirical methods have been proposed. In this respect, either a pseudo-toughness value, K_c , or flow stress theory is applicable, depending upon the fracture mode (brittle, brittle/ductile, ductile). The pseudo-toughness value, K_c , is an equivalent critical toughness parameter for a piping application. It is derived by modifying elastic fracture mechanics solutions of a flawed plate through curvature correction, plasticity consideration, and extensive experimental pipe rupture data correlation. When pipe failure is dictated by gross plastic yielding, a flow stress theory is derived by assuming that pipe instability is governed by the limit load of the pipe.

It will become apparent in subsequent sections that these semi-empirical methods are easy to use but do not assure good correlation with the actual pipe test results.

3.2.1 Axial Cracks

For an axial crack in gas transmission line pipe, equation (2) has been proposed [23] to compute K_c .

$$K_c^2 = \frac{\pi c \sigma_h^2}{\cos \theta} \left[1 + 1.61 \frac{c^2}{Rt} \right] \left[\frac{4 - K}{2} \right]$$
 (2)

$$K_c^2 = \frac{\pi c \sigma_h^2}{\cos \theta} \left(M^2 \right) \left[\frac{4 - K}{2} \right], \tag{2a}$$

where

 K_c = critical stress intensity, ksi $\sqrt{\text{in}}$.

c = half axial through-wall crack length, in.

R = average radius of vessel, in.

t = wall thickness, in.

$$\theta = \frac{\pi}{2} \frac{\sigma_h}{\sigma_c}$$

 $\sigma_h = \frac{Pr}{t}$, nominal hoop stress at failure, ksi

P = vessel failure pressure, ksig

r = inside radius of vessel, in.

 σ_c = failure stress for unflawed vessel, ksi $(M\sigma_h \text{ was used for this value})$

 $K = (3 - 4\nu)$ plane strain; $(3 - \nu)/(1 + \nu)$ plane stress

ν = Poisson's ratio

M = stress magnification factor for an axial through crack in a cylinder which is a function of λ (see Figure 10; M_{exact} exact was used herein)

$$\lambda^2 = \frac{c^2}{Rt} \sqrt{12(1-v^2)}.$$

For axial cracks in an intermediate wall thickness vessel or pipe, Folias [24] and Goodier & Field [25] proposed equation (3) for low to medium toughness materials with relatively long crack. Hahn [26] derived equation (4) for high toughness materials with short cracks.

$$K_c = \sigma^* \left[\frac{8c}{\pi} \ln \sec \frac{\pi M \sigma_h}{2\sigma^*} \right]^{1/2}, \tag{3}$$

where

 σ^* is the flow stress of the material, which according to Hahn can be taken as 1.04 σ_y + 10.0 (ksi) or with less accuracy by 0.51 ($\sigma_y + \sigma_u$)

 σ_{ν} = yield stress, ksi

 σ_u = tensile stress, ksi

 $M = \left[1 + 1.61 \frac{c^2}{Rt}\right]^{1/2}$ or from Figure 10 for a better estimate

$$\sigma^* = \sigma_h M \tag{4}$$

where $M = \left[1 + 1.61 \frac{c^2}{Rt}\right]^{1/2}$ or M_{exact} from Figure 10 for a better estimate. The relationship between

equations (3) and (4) is illustrated in Fig. 11. It is seen that equation (4) is the upper limit for the high toughness (ductile) behavior.

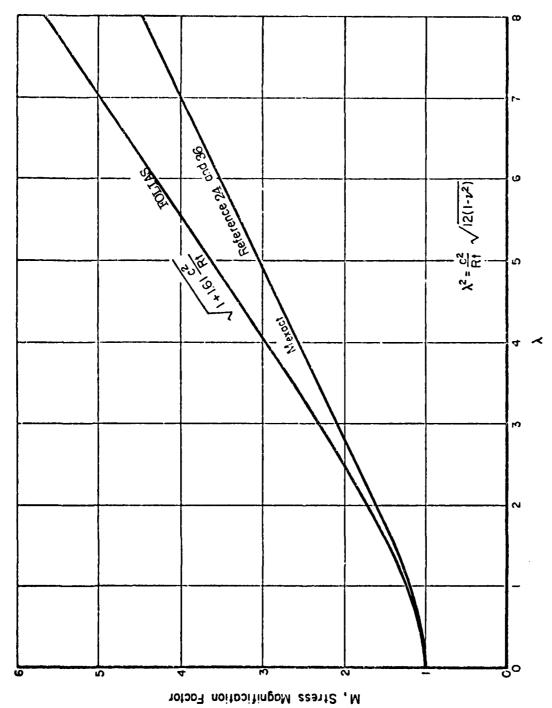


Fig. 10—Relationship between λ and stress magnification factor M

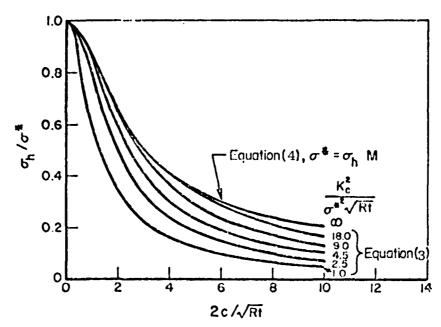


Fig. 11-Dimensionless failure curves for Eq. (3) and (4)

To describe the failure of low to medium toughness materials, Newman [27] proposed a twoparameter fracture criterion to include material yielding as well as brittle failure. These two parameters, m and K_f , are computed from laboratory test results (N tests) and are related to the net section failure stress S_n , of a specimen having half crack length c, width W, and ultimate strength σ_u .

$$m = \frac{\sum_{i=1}^{N} \frac{S_n}{\sigma_u} \sum_{i=1}^{N} K_{le}^2 - \sum_{i=1}^{N} K_{le} \sum_{i=1}^{N} K_{le} \left(\frac{S_n}{\sigma_u} \right)}{\sum_{i=1}^{N} \left(\frac{S_n}{\sigma_u} \right)^2 \sum_{i=1}^{N} K_{le}^2 - \left[\sum_{i=1}^{N} K_{le} \left(\frac{S_n}{\sigma_u} \right) \right]^2}$$
(5)

and

$$K_{f} = \frac{\sum_{i=1}^{N} K_{le}^{2}}{\sum_{i=1}^{N} K_{le} - m \sum_{i=1}^{N} K_{le} \left[\frac{S_{n}}{\sigma_{u}} \right]}$$
(6)

where K_{le} is the computed elastic stress intensity based on gross section stress S to failure equation

$$K_{le} = S\sqrt{\pi c \sec(\pi c/w)}.$$
 (7)

For plane strain behavior m approaches zero $K_f o K_{le} o K_{le} o K_{le}$ (the plane strain fracture toughness). For notch insensitive materials, m becomes unity so K_f relates failure to the ultimate tensile strength. In the range covered by mixed mode and plane stress fracture, the failure stress is a function of both K_f and m. To account for the curvature effect of a cylindrical structure, Adams [28] proposed a revised failure equation which gives the failure stress, S_{cal} , as

$$S_{cal} = \frac{K_f}{C_c \sqrt{\pi c - sec (\pi c/w)} + \frac{mK_f}{\sigma_u} \left(\frac{Ag}{An}\right)},$$
 (8)

where A_g and A_n are cross sectional area and net section area, respectively. A curvature correction factor, C_c , is defined by:

$$C_c = 0.614 + 0.48\lambda + 0.386e^{(-1.25\lambda)},$$
 (9)

where

$$\lambda = [12(1 - \nu^2)^{1/4}c]/\sqrt{Rt}. \tag{10}$$

Figure 12 [29] illustrates the comparison of equations (2), (3) and (8) for a 42 in., 3 in. wall thickness pipe. Approximations made in equation (8) were $m \sim 1.0$ and $\pi c/w \sim 0.0$. It is noted that for K_c less than 200 ksi $\sqrt{\text{in.}}$, all three equations have similar toughness (K_c) and flaw size (2c) relationship. This observations is encouraging because most reactor piping materials, displaying brittle to ductile transition aperature response, exhibit toughness ranges from 50 to 200 KSI $\sqrt{\text{in.}}$.

Other semi-empirical equations to define piping toughness have been described by Folias [31] and Quirk [30]. However, a detailed assessment program using A 106 B pipe experiments [31] indicated that equations (3) and (4) are the most suitable equations to be used. There is evidence, however, that the scatter of the K_c computation may be much larger than that indicated in Ref. [31] when materials or different pipe sizes are considered. It is concluded that the pseudo-fracture toughness, K_c , can be used as a toughness indication and it is accurate under specific conditions. More discussions on this point will be followed in a subsequent portion of the text.

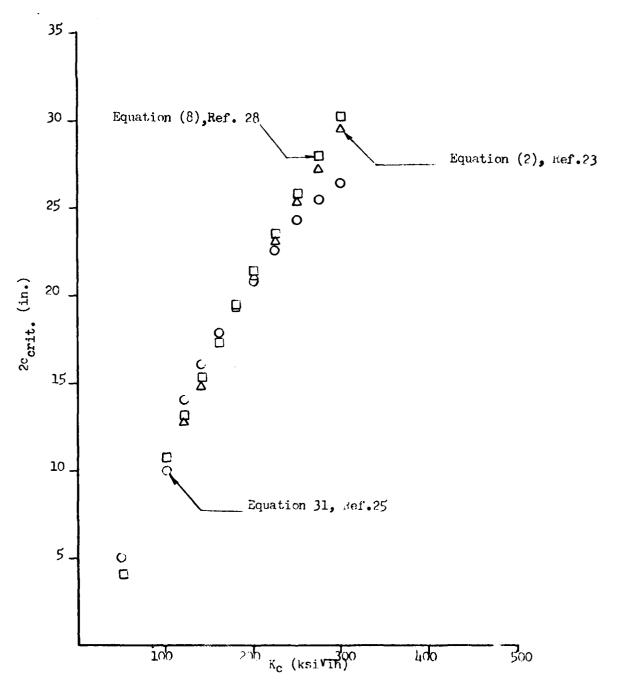


Fig. $12 + 2c_{crit} v_b / K_c$ for a 42 in OD, 3 in wall thickness

3.2.2. Circumferential Cracks

Circumferential cracks can only be initiated and propagated by large axial stress. Therefore, the necessary condition associated with these types of cracks is the presence of high secondary stresses (thermal, bending, expansion and residual stresses). Although most pipe failures in the field are due to circumferential flaws [5], no rigorous analytical method is available to date. Laboratory tests on medium to high toughness materials [32,33,34,35] revealed that for short circumferential flaws the propagation was axial from the crack tips. This result indicated that prototype tests were not good simulations to account for the complicated stress state and microscopic material degradation of the materials in service. However, when longer circumferential flaws were studied, circumferential propagation was observed. In this case, tests on high toughness materials seem to correlate well with an ultimate strength theory. This theory suggests that pipe rupture is produced when the axial stress, due to pressure and bending, reaches the material ultimate strength. The bending stress in the pipe is derived by accounting for the shifting of the section's neutral axis due to the presence of a flaw. One of the formulations [3] gives the corresponding limit moment (Fig. 13) as:

$$M = \frac{4(\pi - \alpha)^2 R_m^2 t^2 \sigma_0^2 - \pi^2 R_c^2 P^2}{2(\pi - \alpha)^2 R_m^2 t \sigma_0} \left[R_0^2 \left(2\cos\beta - \sin\alpha \right) \right]$$
 (11)

where

 σ_0 = flow stress

 R_m = mean radius

 R_i = inside radius

 R_0 = outside radius

T = thickness

P = internal pressure

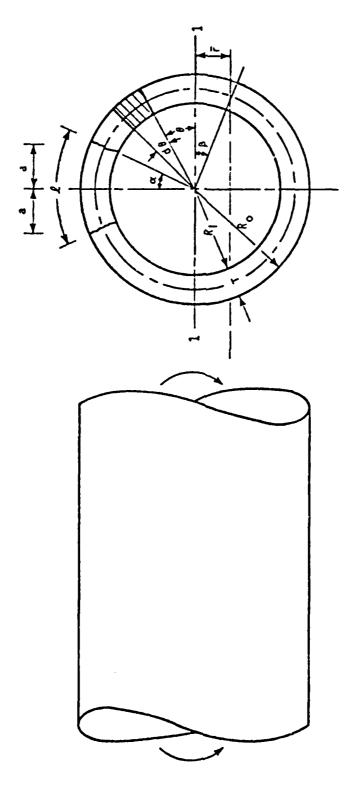


Fig. 13—Pipe with a through wall crack in bending

Another method that may be useful is the solution developed by Erdogan and Kibler [36]. In their work, stress intensity factors have been computed as a function of the parameter λ (Eq. 10). The cylinder is subjected to both axial and bending loads. However, lack of a plastic zone correction factor renders their formulation somewhat unrealistic.

3.3 Semi-Empirical Methods Correlation

The adequacy of the proposed semi-empirical methods are highly dependent on the material being considered. Namely, the pseudo-toughness method, K_c , is for medium to high toughness materials, whereas the flow stress theory is suited for high toughness material applications. In the following discussion, correlations between analysis methods and experimental test data are given for each type of material. Both axial and circumferential cracks are addressed. It will become apparent that both methods can not be used indiscriminately. Lack of good correlation between test data and projections according to the pseudo-toughness, K_c , method raises doubts about the adequacy of this approach. On the other hand, even with limited success, the flow stress theory is still a questionable method to predict inelastic pipe rupture. Specifically, because the flow stress theory is toughness independent and most of all, geometry independent. It is felt that the flow stress theory can be used with success for most of the cases. But before one adapts its methodology, careful consideration should be given to the specific piping system studied and the assumptions and limitations of the theory.

3.3.1 High Toughness Materials

High toughness materials, such as 304 and 316 stainless steels exhibit no brittle to ductile transition temperature and generally fail by ductile rupture. The measured high toughness (Fig. 9) seems to rule out the possibility of brittle fracture initiation. However, cracks have been found in these materials due to various causes. When this material is subjected to heat treatment between 800°F and 1200°F, chromium is depleted from the matrix by precipitation at the grain boundaries in the from of

chromium carbide. The material, having undergone this metallurgical change, is said to be sensitized. When the proper agent, such as oxidizing element, is introduced to the sensitized material, stress corrosion cracking can be developed under imposed thermal and mechanical loads. In this case, the objective is not only to devise techniques to reduce stress corrosion possibility, but also to evaluate the piping stability due to the presence of critical flaws in various orientations.

It has been suggested [37,38,39,40] that the flow stress theory (Eq. 4) may be an adequate method in predicting ductile fracture failure of high toughness materials. As suggested in the following sections, the limited experimental results appear to correlate well with the theory. However, because no crack-tip parameter is considered in the formulation, it is premature to conclude that this theory is applicable regardless of piping geometry or applied loads. Also, Tada and Paris [65] have demonstrated, using J integral techniques, the importance of pipe length/diameter (L/R) ratio in a ductile stability analysis of a circumferential crack in reactor piping.

3.3.1.1 Axial Cracks

Battelle [37,38] carried out 4 experiments on 24 in. diameter 316 stainless steel pipes of 1.5 in. thickness. The length of these pipes was between 8 to 22 ft. The pipes were heated between 470-680°F and pressurized to 5000 psi to induce failure. Both surface cracks and through-wall cracks were introduced in the specimens (Fig. 14). Using equation (4), corrected for reductions in area due to existance of surface flaw, the flow stress equation becomes [37]

$$\sigma_h = \sigma^* \frac{t/d - 1}{t/d - 1/M} \tag{12}$$

where σ_h is the hoop stress at failure; σ^* is the flow stress; M is the stress magnification factor as defined in Fig. 10; and, t and d are pipe thickness and flaw depth, respectively. When very long flaws are considered, 1/M approaches zero and the equation (12) is reduced to

$$\sigma_h = \sigma^*(t-d)/t. \tag{13}$$

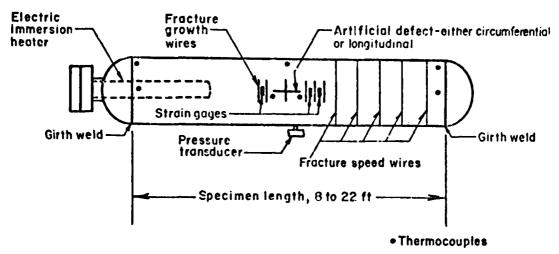
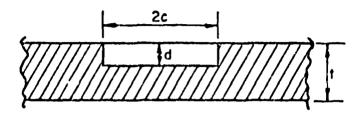


Fig. 14-Type A specimen configuration

In this case failure stress is proportional to the remaining ligament thickness. On the other hand, when deep flaws are considered, equations (12) reduces to the flow stress equation (4) for through-wall cracks. Figure 15 illustrates the correlation between test points and computed values; and it is evident that good agreement was obtained. Since 316 s.s is a very high toughness material, even at room temperature, gross plastic deformation before failure is expected. Therefore, for the pipe geometry studied, the flow stress criterion is adequate.

3.3.1.2 Circumferential Cracks

To investigate the austentic stainless steel toughness against circumferential flaws, Battelle [39,40] undertook a series of experiments performed on type 304 stainless steel plate and pipes. Flat plate specimens containing center cracks were used to evaluate the effect of HAZ (sensitization) and crack tip sharpness on the gross behavior of the material. It was found that extensive blunting practically overshadows the effect of initial crack tip geometry on the final instability. Also, the propagation characteristics were very similar in HAZ and base metal. Because the exhibited high toughness values of 304 s.s., the results from the plate tests suggested that the flow stress theory is an adequate criterion



IDEALIZED SURFACE FLAW CONFIGURATION FOR EQUATION (12)

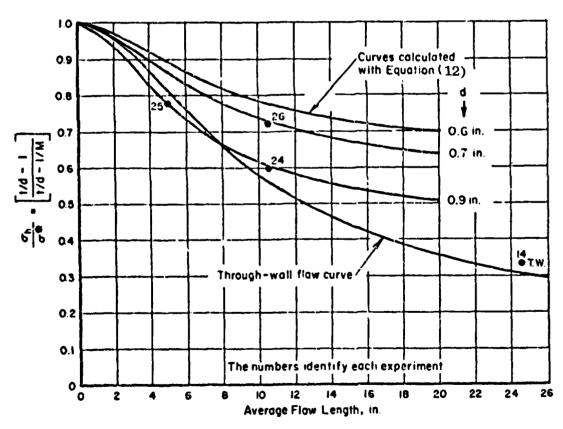


Fig. 15—Surface flaw behavior in 24 × 1.50 Type 316 stainless steel pipe

to predict collapse loads. Ultilizing the computed flow stress values from the plate tests and equation (11), the limiting moment versus flaw length relationship is plotted for internal pressures of 1050 psi and 2500 psi (Fig. 16). Experimental points were obtained from full-scale pipe experiments on two 4-in.-diameter schedule 80 type 304 stainless steel pipes. Initial circumferential flaws subtended arcs over 135° and 75.8°, and testing was performed at a temperature of approximately 3°C. A good correlation between test results and flow stress projections was observed.

For the case of surface cracks, equation (12) can be modified by including the ligament area in the derivation of the cross sectional area characteristics [38].

3.3.2 Medium to High Toughness Materials

In nuclear piping applications, this type of material exhibits a brittle to ductile transition temperature. It can be considered as high toughness material when it is operated at or above the shelf temperature. Therefore, the failure modes, and consequently the analysis methods, are temperature dependent. For this reason, more sub-scale and full-scale experiments have been performed on piping and vessels of this type of material. It is evident from the discussion presented in following sections, that there are a number of technical questions which remain unanswered. The limited evidence to date indicates that when these materials are operating at or above shelf temperature flow stress theory (Eq. 4) is adequate in collapse load prediction. Nevertheless, the inherent simplicity in the flow stress theory (Section 3.3.1) prevents one from adopting this theory for arbitrary pipe geometry and the imposed system loadings. When the operating temperature drops into transition region, the pseudo-fracture toughness, K_c , method may be used for selected axial flaws; however no adequate analytical solution currently exists for circumferential cracks. Furthermore, the poor correlation between K_c and test data raises the question of the general adequacy of the pseudo-toughness theory for piping analysis. An additional practical consideration that contributes towards the difficulty in analyzing these materials is the scatter in material

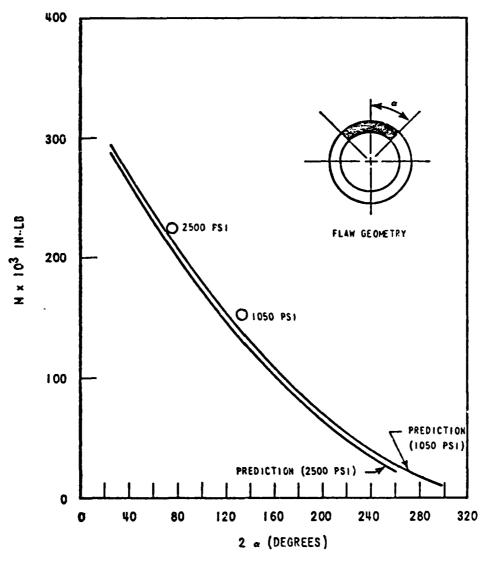


Fig. 16—Comparison on limit moment predictions with experimental results—AISI 304 piping

property data. For materials with identical specifications, significant differences in transition temperature are apparent due to metallurgical variations within a given class of steels. This difference can be observed on the same material from different suppliers or even from same supplier shipped at a different time. Typical materials in this category include A106, A333, and A516.

3.3.2.1 Axial Cracks

For materials containing axial cracks and operating at shelf temperatures, the flow stress theory (Eq. 4) seems to be appropriate for the selected cases investigated. Battelle's [37,38] work on A106 B carbon steel is a typical example of on-the-shelf behavior. A total 22 experiments were conducted on 12.75 in. diameter and 24 in. diameter pipes containing surface and through-wall cracks. These pipes were heated above 450°F under internal pressure (Table 2). According to the Charpy-V-Notch test data contained in the Appendix A [24], 450°F may be considered to be a shelf-level temperature. Figure 17 illustrates the excellent agreement between test point and the flow stress criterion, (Eq. 4).

The on-the-shelf behavior of surface flaws on A106 B steel pipes can also be assessed from other experimental programs. Table 3 contains the test conditions of Battelle's work on surface flaws [37]. To investigate the validity of flow stress criterion, failure stress to flow stress ratios (σ_h/σ^*) are computed for experimental results. Corresponding theoretical σ_h/σ^* values are also computed from Eq. 12 for the d/t rations tested. In Fig. 18 a perfect correlation line at 45 degrees is shown, and the excellent agreement between theory and experiment is noted.

For ferritic piping materials operating in the brittle to ductile transition region, experimental data have been generated to characterize the fracture response. General trends have been observed for specific materials and specific pipe geometries. Figure 19 illustrates the failure stress vs. temperature relationships generated from UKAEA data [5,41] (Tables 4, 5) on 0.36% carbon steel. It is noted that 6-in.-flaw failure stress curve crosses the yield strength curve at 135°F, whereas larger flaws push the crossover point to higher temperatures. Because smaller flaws produce full ductile rupture at lower temperature, this implies that smaller flawed structures have lower transition temperatures. GE results [5,42] on schedule 40 A106 B pipe at room temperature (Table 6) indicated that larger pipe have higher

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Höop Stress Yield Ultimate Outside Wall hsi ksi in. λ 13.49 33.0 75.4 12 1.735 5.08 19.74 33.0 75.4 12 1.674 3.90 19.74 33.0 75.4 12 1.674 3.98 16.43 30.6 75.0 12 1.674 3.94 17.05 30.6 77.9 12 1.64 3.94 17.05 30.6 77.9 12 1.64 3.94 17.05 32.6 77.9 12 1.64 3.94 22.50 34.1 81.5 12 1.64 3.94 22.50 34.1 81.5 12 1.64 3.94 22.50 34.7 12 1.64 3.94 22.50 37.5 74.7 12 0.700 4.65 23.55 36.5 74.7 12 0.700 0.700 4.54				Total Axial	d h, Nominal		e Data				, κ _c (a)	•6	
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21 605 2.5 39.0 42.8 74.0 6.375 0.710 Averages 42.8 74.0	Ci	22	538	5.25	24.8	42.8	74.0	6.375	0.707	2.32	148	43.8	4.55
	C10	21	605	2.5	39.0 Averages	42.8	74.0	6,375	6.710	1, 10	164	42.9	12.0

TABLE 2 CRITICAL CRACK EXPERIMENTS ON CARBON STEEL PIPE WITH THROUGH-WALL FLAWS

(a) $\sigma_{\rm C}$ was taken as $(\sigma_{\rm U}+\sigma_{\rm y})$ /2.4.

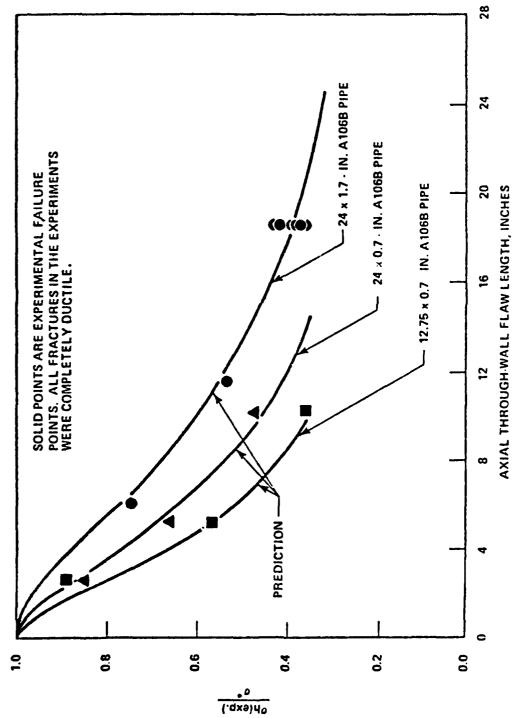


Fig. 17—Comparison of experimental critical flaw size data with calculated behavior for three pipe sizes

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					Wall	Experimental	Average	Flow Stress, σ^* , ksi	,		Predicted Hoop Stress
Pipe	Pipe - Experiment	Test Temporature, F	Surface Length, in,	Oepth, d, in,	Thickness, t, in.	Hoop Stress at Failure The ksi	Crack Lengtin(a) in.	Based on Equation(12)	Eased on Tensile Tests (b)	Failure Mode	at Failure (c) Based on Equation (12) ksi
ខ	4	968	23.4	1.30	1,703	15.1	27.18	49.6	45.4	Break	13.8
ರೆ	ထ	969	24.5	1.27	1,720	16.7	23.24	48.3	45.4	Break	15.8
გ	6	584	24.5	1,45	1,650	8.5	23.21	49.8	45.4	Leak	7.8
ខ	15	623	11.6	1.05	1,619	27.6	10.37	46.8	45.4	Break	25.5
ర	80	469	10, 25	0,355	00.100	26.2	9, 39	41.4	46.0	Break	29, 1
రొ	20	\$0.5	۲. 23	0,350	0.682	32.5	4.33	42.5	46.0	Break	35, 1
S.	24	58.4	11.6	0.900	1.500	22.5	10.55	37.0	35.6	(p) troil	21.6
\$1	25	670	6.0	006.0	1.500	28.4	4,95	36.0	35, 1	reak	27.7
Sı	26	670	11.6	0.700	1.500	25.1	10.51	35.2	35.1	Break	25.2

TABLE 3 EXPERIMENTAL AND PREDICTED FAILURE STRESSES FOR SURFACE FLAWS

(a) Decause these flaws have semicircle ends, the average crack length was determined such that the flaw area and depth remained the same.
 (b) (Q₁₁ + Q₁) /2.4.
 (c) Predicted stresses are based on G* from tensile test results.
 (d) This leaked because Grat, was too low.

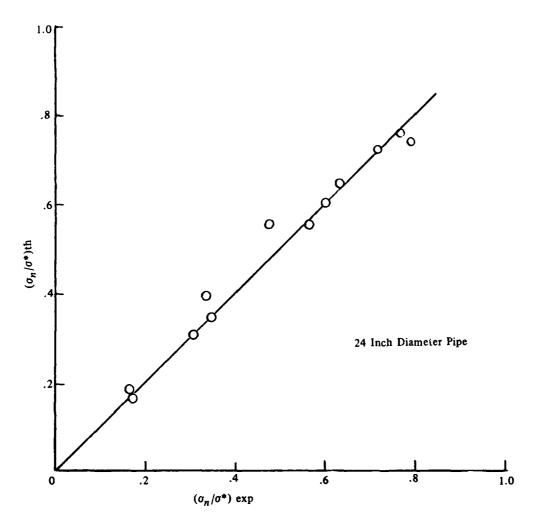


Fig. 18—Experimental/analytical correlation of surface flaws on A106B pipes (refer to Table 3).

(On shelf behavior),

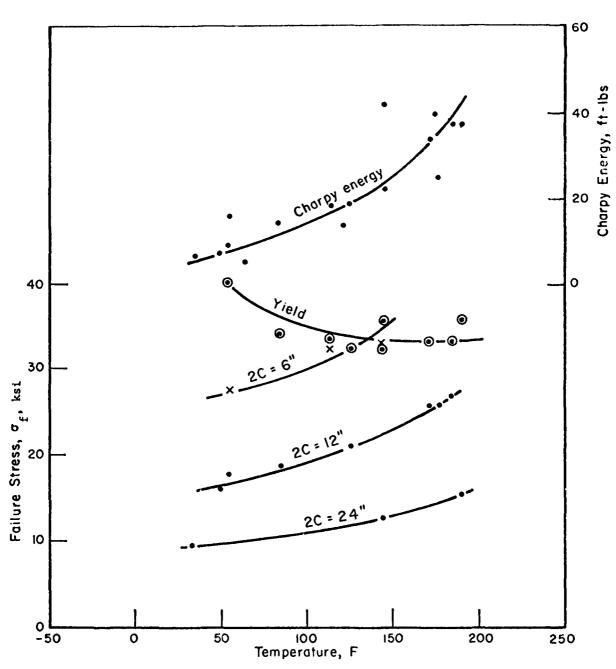


Fig. 19—Relationship of failure stress, Charpy energy and yield strength with temperature for UKAEA 0.36 percent carbon steel pipes

TABLE 4. WARE AREA THROWST-WALL PLAN DATA ON STREE CYLLIDIREAL VESSELS

Section Circles Section 19, 19, 19, 19, 19, 19, 19, 19, 19, 19,														
ינות ממיי ממיי ממיי		1016. 101	Ultimate, hei	Eleag. percent	j.*	inches 2	1,40	P-Deceile	٣Ę	۔ وارڈ	tir Cb.	r	ž	Type of Steel
מנה מנה	9.0	86.8	(69.7)(6)	11	13.5 23.6	77.88 12.89	25		3.5	(3.01)	••	2:	7.	0,36% C steal , NOT +60 F to +85 F
, and	0.7	(9. 70	(6.7)	4	17.5	13.00	121	•	:	9	•		::	
	1.0	1.03	70.1	?	27.6	8.	*	-	1.10	7. 25	۰	1.13	7.4	•
**************************************	99	3.5	2.7	22	32.4	8.8	23		2.	17.7	2		0.0	a (
	!	1	;	;	•	3	!	}	2		•			•
ייי	9.7	34.0	1.,1	22	18.7	12.00	1		2.21	3.6	•	1.39	19.6	•
	9	 	43.4	2	21.0	12.00	125	-	17.7		•			•
	2.	27.	4.	9 :	23.0	12.00	2	4	2.7	2.69	20		6.03	•
				2 :	26.7	2.00	3:	۵,	7.7	2.69	•	\$		•
40771			(6.5)	; ;	•	3.5	2 5	• •	7.7	3.63	•		2.	• •
41:14		÷.*.	6.5	:	2.5	900	2 2	• 6	7.7		9 0		? ?	
•	9:	42.1	-3	7	29.6	12.00	3	Δ.	7.71	2.13	• •		7.7	Alternative Control of 151 C. 155 -4 F
25	0.7	(22.9)	(4).2)	::	31.4	2.00	i	۵	7.7	(4.1)	2		50.4	Ditte
	2.	• 6	C 2	3	29.3	12.00	20	Α.	2.21	2.13	•		4.64	
1,00	2.5		(2.5)	: :	9.1.6	2.00	21	۰ م	2.21	(1.99)	2	1.39	20.4	•
•	:	•	:	}	• 67	8.7	102		3 .21	2.26	•		6.5	\$1-tilled eteel 0.161 C, MPT -63 F
11.0	9.2	35.0	79.7	2:	13.7	24.00	571	•	3.	4.28	•	3.6	33.1	0.36% C steel
	2.			\$;	13.3	8.5	06.7	۰	4.42	5.23	2	3.5		0.362 C steel
3		200		: :		8.8	•	٥.	3	(); ();	2 4		2	Al-grain-refined eteel 0.DX C
47:10	0.	2	2	::	4 02	9. 7.	;	• •	3		•			Low alley steet 0.1332 C
410	1.0	(72.8)	(3.26)	;	7.0	24.00	; c	۵.	13	(3. (3.	. 0	5		•3310
E	9.1	(94)	(45.7)	;	:	24.75	22	-	4.56	(7.18)	•	2.68	23.0	0.36% C steel
W126 66	0.1	(3.6)	(92.1)	;	13.2	29.00	ğ	-	\$.34	(9.98)	•	8.8	£0.2	Low alloy steel 0.1555 C
•	•	04.40	(69.7)	;	10.1	12.00	2			3	•		:	
7771	0.1	Q	(69.7)	,	27.1	12.00	176			a.s.)	•		36.2	0.36% C steel
					Sheekes Anelysis of Teet Haterisha, veight, percaps	the of Test	Hateriele	POLENE POPER	**					
			•	ı	Na . 8t	•		•	ĸ	8	2	8	•	_ [
	0.36 %	U	9.36		0,64-0.66 0.10-0.13	0.038-0.024	0.024	0.015-0.026	۱ ا	:	;	:	•	
	Al-grafa-re	in-refined ages	Canl 0.13		0.14 0.13	0.033	33	0.00	:	:	:	:	•	•
	\$61114-18	led atesl	97.0		1.22 0.20	8.0	2	410.0	i	:	:	:	:	
	Lorelloy .	ley ates!	0.155		1.30 0.22	0.03	2	0.022	0.23	3.	0.155	0.0	9.8	8

B.S. 1501-151, NOT of +32 F. 75 ft-1b charpy shelf energy Ditto 0.36% C Steel, NDT of +68 % to +77 % 60 fc-1b charpy shalf energy Ditto Type of Steel TABLES. AKIAL THEOUGH-WALL FLAW DATA ON STEEL CTLINDRICAL VESSELS EXPERIMENTS CONDUCTED BY UNAEA ئر. 1.17 1.17 1.58 1.58 1.58 1.58 ×, <2.40 ءًام 6.14 6.14 99.7 2.32 2.97 1.095 1.095 2.19 2.19 2.19 4.38 Charpy Energy, ft-1be 422 2.3 2.3 2.3 52 7.5 22 22 22 23 \$ 220 on s Test Tempera-ture, 194 122 50 -22 -23 -29 -29 194 122 46 46 16 16 -22 -18 Flav Length, inches 12.00 12.00 12.00 12.00 9.00 12.00 12.00 12.00 12.00 24.00 12.00 12.00 12.00 **6**.00 6.00 24.90 24.90 24.90 Burst Hoop Stress Flaved, kei 29.9 27.0 22.2 21.3 19.5 20.6 29.6 28.8 23.7 19.7 11.11 Held, Ultimate, Elong, kai kai percent 1 2 2 2 2 1 Tensile Stress Data 7.06 28.7 31.6 31.7 38.5 74.1 72.8 70.1 45.5 73.2 Mall Dismeter, Thickness, inches inch 99999 0.7 Spectors Number

Steel		35	*	۵.	Mn W1	P Mn #1	1	Cr No		Renarks
0.36% C normalized		0.10/0.22	0.35/0.36 0.10/0.22 0.038/0.047 0.012/0.024	0.012/0.024	97.0/77.0					Lange of analysis of two casts
8.5.1501-151 AB-rolled	0.25	0.045	0.028	0.00	0.70					Plate analysis
Mo-B normalized	0.12	0.35	0.023	0.014	0.77	0.03	0.03	94.0	0.00	Place analysis

Properties of Steel Plates

3.26 1.36 2.15 2.72 5.60 3.15 5.88 5.28 5.28 2.85 3.41 5.66 3.14 3.14 3.74 6.25 10.1 Equation (2), ksi vin. K_c(c), Based on 200 195 154 154 152 163 153 158 149 183 139 139 141 165 119 121 121 138 $\frac{\sigma_{11}+\sigma_{2}}{2.4}$ \$ 0.04 47.0 47.0 47.0 52.8 52.8 52.8 52.8 Ultimate 6.99 66.9 6.99 76.3 76.3 76.3 76.3 68.3 68.3 68.3 66.9 66.5 66.5 66.5 Tensile Test Data, ksi Yield 47.4 47.4 47.4 41.4 46.5 47.4 46.5 50.3 50.3 50.3 50.3 50.3 44.3 44.3 4. 4. w. w. Strength from Vessel Equation (3), Test(b), NA 85.50 85.80 85. 61.2 61.2 61.2 61.2 69.4 69.4 69.4 69.4 ksi Calculated 45.8 36.5 38.2 52.5 42.0 49.8 46.3 47.0 49.0 50.3 54.3 53.6 39.7 41.5 45.5 44.6 ksi Failure Stress, 10.3 13.4 21.0 20.3 31.9 14.7 19.3 28.1 38.4 27.8 29.1 11.1 19.6 ksi Length(a), Flaw 5.00 4.32 3.27 2.24 3.27 2.00 1.50 0.75 0.75 5.00 4.76 2.50 1.50 0.75 4.75 3.49 2.25 1.01 Ë Thickness, Temperature, 09 09 09 09 09 88888 8 8 8 8 0.430 0.430 0.430 0.431 0.429 0.430 0.430 0.32 0.32 0.32 0.32 0.32 0.71 0.71 0.71 0.71 5 Diameter 8.66 8.66 8.66 8.66 8.66 12.75 12.75 12.75 12.75 6.67 6.67 6.67 6.67 6.67 6.67 6.67 5 Specimen 6-32F 6-30F 6-31F 6-33F 6-35 6-35 6-38 6-31 8-34 8-32 8-31 8-30 12-30 12-32 12-33 12-31

TABLE 6. THROUGH-WALL FLAW DATA ON A106B PIPE FROM REYNOLDS

(a) All flaws were through-wall flaws.

⁽b) It is not known if these burst tests were conducted on these lengths of pipe or on other lengths from the same heat. NA = not available. (c) σ_c was taken as $(\sigma_u + \sigma_y)/2$.4.

tolerance to the existence of larger axial flaws (Fig. 20). To date, macroscopic observations and analytical solutions have been able to establish flawed structural behavior with limited success. Specifically, a non-dimensional parameter β seems to be one of the variables that can be ultilized to correlate the laboratory results. The shape parameter, β , is defined by:

$$\beta = \frac{2c}{\sqrt{Rt}} \tag{14}$$

where

2c = flaw length

R = pipe radius

t = pipe wall thickness

To test this assumption, a correlation between failure stress and β is made on Fig. 21 [37]. On this graph (all test data are reproduced in Appendix A), the flow stress theory (Eq. 4) is shown as solid lines and McDermott's [43] limit analysis is shown as dotted lines. A general trend is seen, but the scattered data points signal the importance of other variables which have not been incorporated into the definition of β .

As stated previously, the uncertainty in as-received material properties, flaw geometry, pipe size and pipe geometry play a very important role in the precise location of the brittle to ductile transition temperature of a specific structure. When the temperature is below NDT, LEFM is adequate and when the shelf temperature is reached, flow stress criterion may be appropriate. However, in the transition region, mixed mode of failure occurs. The degree of ductility associated with failure is affected by various factors and it is very difficult to express fracture response in the framework of present elastic/plastic fracture mechanics technology.

Among the existing criteria, pseudo-toughness (K_c) and flow stress (σ^*) theories seem to be favored by researchers because of their simplicity. However, if a material fails in mixed mode manner,

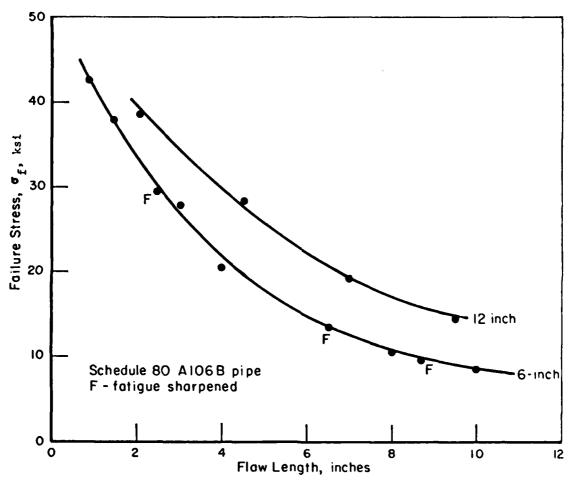


Fig. 20-Effect of pipe size and notch acuity on axial through-wall flaws in schedule 80 A106B pipe

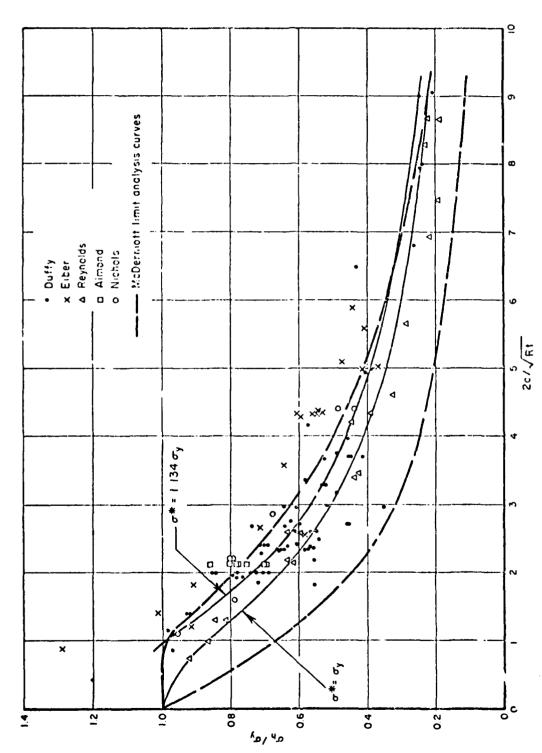


Fig. 21-Analytical curves and 122 ductile-fracture data points for pressure vessels containing through-wall axial flaws

application of the flow stress theory is tenuous due to its underlying assumption of full ductility. On the other hand, the pseudo-toughness formulation has the capability to rigorously treat brittle failure and also incorporates a plasticity correction. Unfortunately, the semi-empirical nature of K_c requires extensive experimental data to justify its validity and also limits its ability to extrapolate to different marerials, structures, and service conditions. To test the adequacy of K_c and flow stress criterion, test data from UKAEA (Tables 4 & 5) and GE (Table 6) have been used to compute K_c , σ^{\bullet} , the results are shown in Figs. 22 and 25. If the pseudo-toughness, K_c , can be considered as a criterion, it should be a constant for different flaw lengths (geometry independent). Similarly, if the flow stress criterion is workable, a close correlation should exist between the flow to failure stress ratio, $\sigma^{\bullet}/\sigma_h$, and the M factor (Eq. 4). Unfortunately, the expected behavior is not apparent in these figures.

For the case of surface flaws, complexities similar to those for through-wall flaws also exist. However, it has been pointed out by Kiefner [5] that surface flaws have much lower transition temperature than through-wall flaws. This is a reasonable observation because the ligament is subjected to much less constraint than a full thickness section. Consequently, for the same material operating at the same temperature, surface flaws are more likely to undergo ductile rupture rather than a through-wall flaw. Unfortunately evidence on testing of A106 B pipes [34] having inner or outer surface flaws does not substantiate this suggestion (Tables 7, 8). The flow stress, computed from the equation:

$$\sigma^* = \frac{\sigma_{\text{yield}} + \sigma_{ult}}{2.4},\tag{15}$$

ranges from 44 ksi to 45 ksi. If the surface flaws behave in ductile manner, $M_p \sigma_h$ values on these two tables should be within this range in order for the flow stress theory (Eq. 4) to hold. Figures 26 and 27 summarize this comparison and two observations are noted. First, the scattered data points indicate lack of correlation; and second, the definition for the "flow stress" is not optimal. If the constant 2.4 in the above equation is reduced, i.e. higher flow stress is computed, better correlation can be attained. In

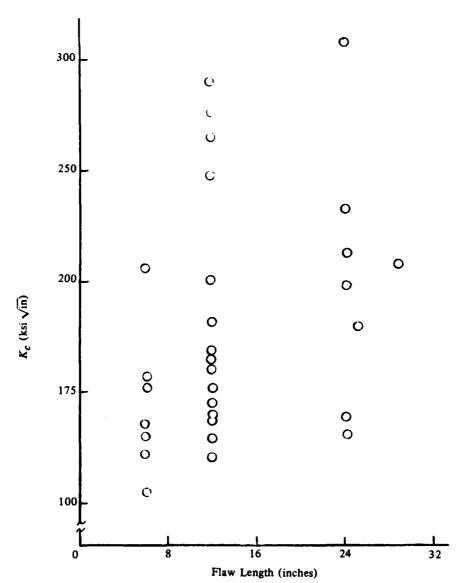


Fig. 22-UKAEA axial through-wall flaw

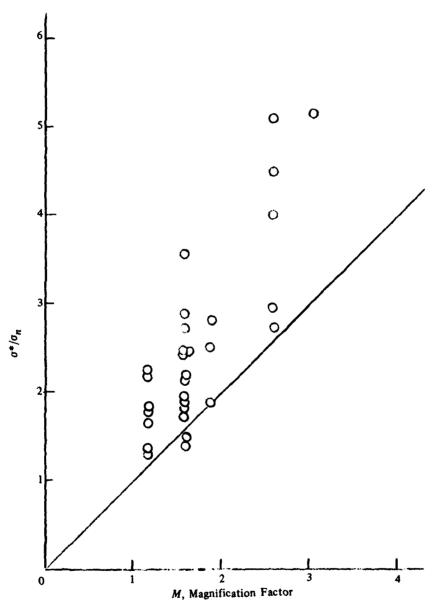


Fig. 23-UKAEA axial through-wall flaw

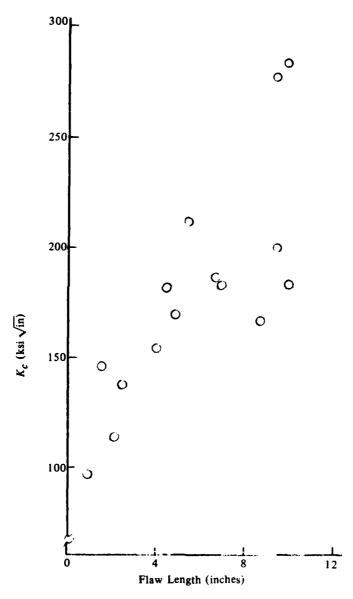


Fig. 24-GE axial through-wall flaw

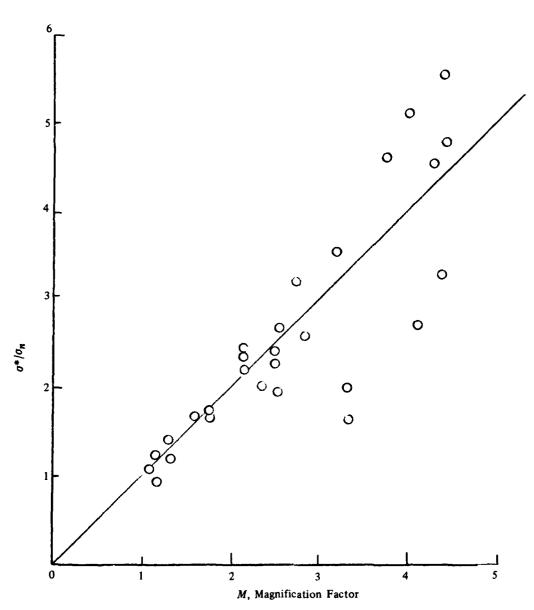


Fig. 25-GE axial through-wall flaw

80.00 68.23 104.79 772.31 772.31 76.89 772.31 772.31 772.31 772.31 772.08 63.68 63.68 63.69 63.63 63 63 63 63 63 63 63 63 63 63 63 6 ν, K 25.05 .۾ 41,522 52,522 52,522 53,523 53,533 Դ **e** 1.50 1.35 1.35 1.29 1.29 1.62 1.62 1.33 1.33 1.33 1.68 1.68 ع ام 2c /RE 0.65 0.32 0.32 0.50 0.50 0.53 0.17 0.40 0.40 0.17 0.27 0.27 0.73 10 m Length, inches 2c 2.00 4.00 8.00 3.00 5.03 6.12 111.31 8.16 8.16 8.16 7.00 4.89 4.89 3.00 4.89 Flaw Data Depth, 0.139 0.335 0.216 0.231 0.243 0.261 0.046 0.046 0.326 0.116 0.035 inch d Hoop Stress at Failure, ksi Ultimate, ksi Data 733.88 735.88 75 Tensile Stress Yield, ksi Specimen Number Test Number

TABLE 7. AXIAL INSIDE SURFACE FLAW DATA ON A106B PIPE, 6 INCHES, SCHEDULE 80, 0432 INCH WALL

Flavs cut with 2.75-inch diameter milling cutter, 45 degree included angle, 0.010-inch tip redius.

Test Perperature ~ 60 degrees F.

(a) Used ultimate tensile for 0 b.

## Speciaen Yield, Ultivate, willingt, willingt, will will will will will will will wil				1608:16 Data	noop or con		Flav Data								
6-10 56.5 58.5 47.2 0.1112 23.00	Test Member	Spectmen Number	Yield, kei	Ultimate, ksi	kst kst o _i	Derth.	Length, inches 2c		Lesk Failure,	Aln	20 78.	୍ଧୀ ଚ	χĻ	×	ېژ
6-11 56.5 58.5 27.2 0.230 1.75 0.230 1.75 0.230 1.75 0.230 1.75 0.230 1.75 0.230 1.75 0.230 1.75 0.230 1.75 0.230 1.75 0.230 1.75 0.230 1.75 0.230	-	61.10	5	28.5	61.2		23.00			,	9	:			
6-2 56.5 58.5 44.8 0.230 1.75 6.1 1.51 1.11	• ^			, a	27.2	711.0	20.00	•		9:	19.09	0	:	:	:
6-1 (4)-5 (5	. ~				. « //	2520	7	• .	•	:	7.67	7.15	: 3	; ;	: }
6-5	٠ ٠		? .	200	2	0.50	0.00	, ه		?!	1.51	1.31	1:31	1.27	56.76
6-5 (4), 5 (8), 5 (1), 6 (1), 7 (1), 8 (1), 9 (1),	• ~	7.9	44.3	2,000	7.00	0.230	9.00	0 4			3.46	1.66	2.15	1.60	26.44
6-12 (7.7) 58.5 21.0 0.121 26.00 b L68 22.48 2.79 6-13 (7.7) 58.5 24.0 0.125 26.00 b L68 22.48 2.79 6-14 (7.7) 58.5 24.0 0.125 800 b L68 22.48 2.79 6-24 (7.7) 58.5 24.0 0.125 8.00 b L68 22.48 2.79 6-24 (7.7) 58.5 24.0 0.125 8.00 b L68 6.92 3.03 3.75 6.40 6.40 0.126 8.00 b L88 6.92 3.03 3.75 6.40 9.124 8.00 b L88 6.92 3.03 3.75 6.40 9.124 8.00 b L88 6.92 3.03 3.75 6.40 9.124 8.00 b L88 6.92 1.13 3.75 6.40 9.124 8.00 b L78 1.13 5.14 1.13	۰.		5 67	28.5	37.5	572.0	20.4	•				96.1	7.7	7.04	0.70
6-13 47.7 58.5 24.0 0.235 26.00 b L		6. 12	67.7	5.85	21.0	0.321	26.00	2 .	p.1		37.6	7.00	61.7	1	· ·
6-8 477 58.5 29.2 0.235 8.00	co	6-11	47.7	58.5	24,0	0.295	26.00	م ه	נ, ו	89	22.48	2,44	: :	: :	: :
6-9	۰	8-9	47.7	58.5	29.2	0.235	8,00	•	,,	3,5	6 9	2	7.5	78	17.
6-40 52.1 65.4 46.9 0.108 8.00 1	91	6-9	47.7	58.5	19,3	0.345	8.00	•		80	6. 92	86	,,,	5	200
6-41 52.1 65.4 49.0 0.108 8.00	11	9-40	:	58.5	10.4	0.382	8.00	•	.1	88	6.92	5.63	3.75	6.38	
6-42 52.1 65.4 46.9 0.124 5.00	2	17-9	52.1	65.4	0.67	0.108	8.00	•		.25	6.92	1.33	3.75	1.24	9
6-43 32.1 65.4 35.0 0.292 5.00 6.4 4.32 1.87 2.55 1.87 2.55 1.87 2.55 1.87 2.55 1.87 2.55 1.87 2.55 1.87 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 2.55 1.37 1.41 1.39 2.55 1.37 1.41 1.39 2.55 1.37 1.41 1.39 2.55 1.37 1.41 1.39 2.55 1.37 1.41 1.39 2.55 1.37 1.41 1.39 2.55 1.37 1.41 1.39 2.55 1.37 1.35 1.35 1.35 1.37 2.55 1.35 1.35 1.35 1.35 <th< td=""><td>ລ</td><td>6-42</td><td>52.1</td><td>65.4</td><td>6.97</td><td>0.124</td><td>5.00</td><td>4</td><td></td><td>.29</td><td>4.32</td><td>1.39</td><td>2.56</td><td>25.1</td><td>28.88</td></th<>	ລ	6-42	52.1	65.4	6.97	0.124	5.00	4		.29	4.32	1.39	2.56	25.1	28.88
6-44 52.1 65.4 49.6 0.410 5.00	7.	6-43	52,1	65.4	35.0	0.292	2.00	•		.68	4.32	1.87	2.55	2.30	82.14
6-45 52.1 65.4 49.1 0.184 3.00	13	77-9	52.1	65.4	19.6	0.410	5.00	•		.95	4,32	3.34	2.56	12.58	245.62
6-46 52.1 65.4 39.9 0.318 3.00 6 1. 77, 2.59 1.64 1.75 6.46 5.2 6.46 5.2 6.46 5.2 6.46 5.2 6.46 6.2 6.40 6.2 6.40 6.40 6.40 6.40 6.40 6.40 6.40 6.40	15	6-45	52.1	65.4	7.67	0.184	3.00	•		64.	2.59	1.33	1,75	1.32	69
6-43 52.1 65.4 54.5 0.130 4.00 6 L .76 3.46 1.90 2.15 6.49 52.1 65.4 64.5 0.137 2.00 6 L .76 3.46 1.90 2.15 1.41 1.39 6.49 52.1 65.4 62.9 0.037 6.00 L .76 3.46 1.30 1.41 1.39 6.70 52.1 65.4 62.9 0.037 6.00 L .78 1.31 1.41 1.39 1.41 1.39 6.70 5.4 6.7 6.70 1.69 1.87 L .19 10.26 1.27 4.97 1.69 1.62 6.81 53.9 69.2 29.8 0.778 8.12 L .64 7.02 2.32 3.60 6.82 54.4 68.3 1.95 0.136 11.98 L .8 5.4 68.3 1.95 0.136 11.98 L .8 5.4 68.3 1.95 0.136 11.98 L .77 2.60 1.72 1.76 6.80 5.4 68.3 1.95 0.136 11.98 L .77 2.60 1.72 1.76 6.80 5.4 68.3 1.95 0.136 11.90 L .77 2.60 1.72 1.76 6.80 5.4 68.3 1.95 0.136 11.90 L .77 2.60 1.72 1.76 6.80 5.4 68.3 1.95 0.136 11.90 L .77 2.60 1.72 1.76 6.80 5.4 68.3 1.95 0.136 11.90 L .77 2.60 1.72 1.76 6.80 5.4 68.3 1.95 0.136 11.90 L .77 2.60 1.72 1.76 6.80 5.4 68.3 1.95 0.136 11.90 L .77 2.60 1.72 1.76 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.80 5.4 6.8 6.9 6.9 6.9 6.9 6.9 6.9 6.9 6.9 6.9 6.9	.,	97-9	52.1	65.4	39.9	0.318	3.00	•	,3	7.	2.59	1.64	1.75	2.33	58.63
6-49 52.1 65.4 46.5 0.337 2.00	13	67-9	52.1	65.4	34.5	0.330	4.00	9	ы	97.	3.46	1.90	2.15	2.70	93.03
6-50 52.1 65.4 62.9 0.047 6.5011 5.62 11.04 11.17 6.7011 5.62 11.04 11.17 6.7011 5.62 11.04 11.17 6.7011 5.62 11.04 11.17 6.7011 5.62 11.04 11.17 6.7011 5.62 11.04 11.17 6.70 11.18	13	67-9	52.1	65.4	46.5	0.337	2.00	•	.1	.78	1.73	1.41	1.39	1.59	37.75
6-79 55.9 69.2 54.6 0.053 11.87	20	9-30	52.1	65.4	62.9	0.047	6.50	•		.11	5.62	 9.1	3.17	1.03	65.23
6-80 53.9 65.2 41.0 0.185 8.18 a .43 7.07 1.69 3.62 6-81 53.9 65.2 2.9.8 0.278 8.12 a .64 7.02 2.32 3.80 6-81 53.9 65.2 2.9.8 0.278 8.12 a .64 7.02 2.32 3.80 6-83 55.4 66.3 19.5 0.356 11.98 a .82 10.36 3.50 5.40 6.83 55.4 68.3 47.9 0.138 4.92 a .79 2.60 1.72 1.76 6-85 55.4 68.3 3.50 6.36 3.03 a .75 2.50 5.00 6-85 55.4 68.3 3.50 6.356 5.30 a .75 2.50 1.75 1.76 6.85 5.40 68.3 3.50 6.356 5.30 a .75 2.50 1.75 1.76 6.85 5.40 68.3 3.50 6.350 3.03 a .75 2.50 1.77 1.76 6.85 5.40 68.3 3.50 6.350 3.03 a .75 2.50 1.77 1.76 6.85 5.40 68.3 3.50 6.350 3.03 a .75 2.50 1.77 1.76 6.85 5.40 68.3 3.50 6.350 3.03 a .75 2.50 1.77 1.76 6.85 5.40 6.85 5.40 6.85 5.40 6.35 6.35 6.35 6.35 6.35 6.35 6.35 6.35	36	62-9	53.9	69.2	24.6	0.033	11.87	•		.19	10.26	1.27	76.7	1.19	64.83
6-81 53.9 69.2 29.8 0.278 8.12	33	08-9	53.9	69.2	41.0	0.185	8.18	4		.43	7.07	1.69	3.62	1.56	63.63
6-82 51.9 69.2 60.7 0.071 1.02 a .16 2.61 1.14 1.76 6-82 54.4 68.3 19.5 0.136 11.98 a .25 10.36 1.00 5.00 6-84 54.4 68.3 47.9 0.138 4.02 a .32 4.25 1.43 2.51 6.45 6.46 6.51 1.54 0.136 4.00 6.46 6.51 1.54 0.136 6.46 6.46 6.46 6.46 6.46 6.46 6.46 6.	38	9-9	53.9	69.2	29.8	0.278	8.12	•		79.	7.02	2.32	3.80	2.31	63.93
6-83 54,4 68.3 19.5 0.356 11.98 a .82 10.36 3.50 5.00 6-84 54,4 68.3 47.9 0.318 4.92 a .32 4.25 1.43 2.53 6-85 54,4 68.3 39.6 0.340 3.01 a79 2.60 1.72 1.76 6-86 54,5 54,5 58.3 35,5 59.30 a79 2.60 1.72 1.76	39	6-32	53.9	69.2	60.7	0.071	3.8	•		.16	19.2	1.14	1.76	1.08	65.63
6-84 54.4 68.3 47.9 0.138 4.92 a .32 4.25 1.43 2.53 6-84 54.4 68.3 3.9.6 0.134 3.01 a L .79 2.60 1.72 1.76 6-86 54.4 68.3 3.54 0.134 3.01 a L .79 2.60 1.72 1.76	0,	6-83	7.75	68.3	19.5	0.356	11,98	•		.82	10.36	3.50	5.00	.0.4	\$0.5
6-85 54,4 68-3 39-6 0-340 3-01 - 1. 79 2-60 1,72 1,76 7,74 5,74 5,74 1,76 1,76 1,76 1,76 1,76 1,76 1,76 1,76	7.7	78-9	24.4	68.3	47.9	0.138	4.92	•		.32	4.25	1,43	2.53	1.38	61.53
2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	77	6-85	7.75	68,3	39.6	0.340	3.01	•	,.1	.79	2.60	1.72	1.76	2.62	103.72
77.7 7.17 7.10 7.1	53	6-86	24.4	68.3	35.6	0.225	9,37	•		. 52	8.10	1.92	4.24	1.83	65.06

TABLE 8. AXIAL OUTSIDE SURPACE PLAN DATA ON ALGOS PIPE, 6 INCH, SCHEDULE 80, 0,432 INCH WALL

⁽a) Flaw cut with 2.75-inch diameter milling cuttar, 45 degree included angle, 0.010-inch tip radius.
(b) Flaw cut with 0.020-inch thick slitting saw.

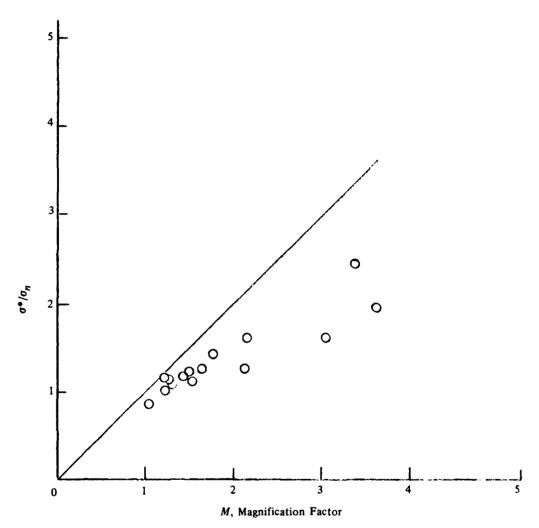
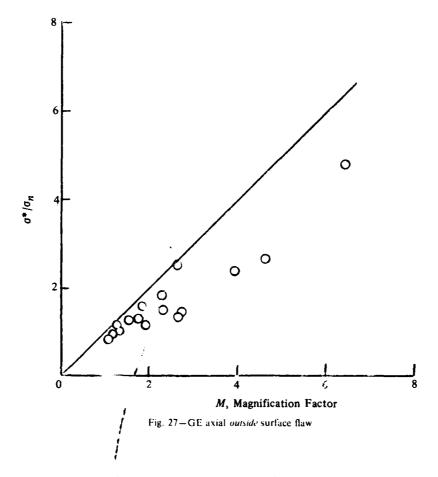


Fig. 26-GE axial inside surface flaw



comparing through-wall flaws (Fig. 25) with surface flaws (Figs. 26 & 27), it is interesting to note that if higher flow stress value are used, the surface flaw results display better correlation. This may indicate the surface flaw have higher ductility, lower transition temperature, as discussed previously.

3.3.2.2. Circumferential Cracks

When a material is operating on the shelf, ductile rupture is expected. The Battelle [38] test on 24×0.75 in. A106 B pipes (Table 9) suggest the same limit load analysis as that used for high toughness materials is applicable. In this analysis, the load carrying capability of the flawed pipe is restricted to the limit load. The applied pressure and bending loads are corrected to the new neutral axis position

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				1	[Calcula	Calculated Data, ksi(c)	ksi(c)					
	•		Flaw	۵		ė	غ		Oflow	Rased on	Bending	Bending Moment Temperature	Tensil	Tensile Test Data ksi
Experiment	net. in.	nom. in.	2c, in.	fail. psig	om.	or.	mon.	σ _B (b)	CL net	of nom.	f(P _f)		5	o C
29	0.175	0.175 0.630-0.757, Avg 0.670	37.75	1070	9.74	9.74 34.5	19.48	20.2	54. 5	23.8	1750P	526	31.8	82.4
30	0.175	0.175 0.627-0.775, Avg 0.702	56. 625	1390	12.17	4.1	24.34	25.3	10.0	36. 6	16902	505	31.8	82.4
33	0.175	0.175 0.658-0.748, Avg 0.700	47.2	940	1.6	30.3	15.2	19.3	49.2	26.9	18402	523	31.8	82.4
33	0.175	0.175 0.621-0.772, Avg 0.695	18.9	1740	14.15	55. 9	28.3	6.9	0	21. 0	10002	534	31.8	82. 4
8. 4.	0.175	0. 656-0. 727, Avg 0. 698	65.8 8	1400	11.35 45.1	45.1	22. 7	19.3 Avg	64.5	30.7	1183P	541	31.8	62. 4

TABLE 9, SUMMARY OF CIRCUMFERENTIAL SURFACE-FLAW EXPERIMENTS ON 24 X 0.150 A106B PIPE C16

(a) These values were calculated using $\sigma_L = Pr/2t_{\rm net}$. (b) These values were calculated using the measured wall thicknesses. (c) σ_L , longitudinal membrane stress, σ_H , hoop membrane stress, σ_B longitudinal bending stress.

due to the existence of a circumferential flaw. The limit load can be computed from the flow stress of the material. Figure 28 is a cross plot of results from Table 9, where both bending moment and failure stress are presented with flaw length. It is noted that maximum bending moment capability does correspond well with minimum failure pressure. This suggests the failure description of circumferential flawed pipes is quantitatively correct.

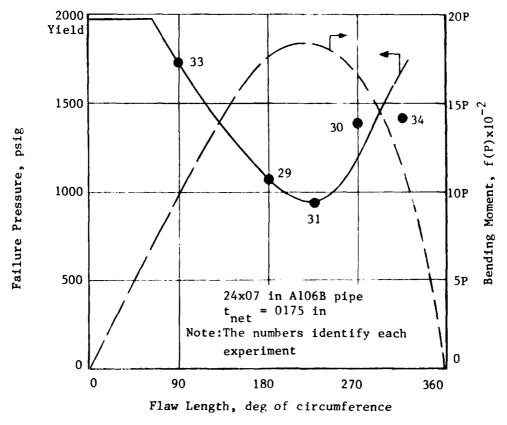


Fig. 28-Failure pressure and calculated bending moments for various circumferential surface flaw length

When the material is operating at room temperature, similar analysis technique may be employed. Test results [45, 46] on 6 in. A106B schedule 80 ripes are tabulated in Tables 10 and 11. To further investigate the adequacy of the limit load theory, a limit moment is computed for 0.0 and 1000.0 psig internal pressure at various through crack lengths (2α) . Solid lines in Fig. 29 represents the computed values using Eq. 11, and test points, represented by circles, are from Tables 10 and 11. A fairly good agreement is noted; however when compared with the high toughness material (304 s.s) predictions (Fig. 16), the experimental result displays a larger deviation from theory.

3.4 Recent Advances in Elastic/Plastic Fracture Mechanics

The pseudo-toughness criterion, K_c , was developed from LEFM theory, modified by a large body of experimental data and it has been applied with very limited success to pipe rupture studies on medium toughness materials operating in the brittle to ductile transition region. Previous discussion has also indicated that the flow stress theory may be utilized to compute fracture behavior of piping made of high toughness materials or medium toughness materials operating at shelf temperature. The desirable situation in a piping integrity investigation is to have material criteria that are a counterpart of K_{lc} for brittle fracture, and are capable of characterizing material at the shelf temperature as well as in transition region.

The importance of recent advancement in elastic-plastic fracture mechanic is not only to provide a better understanding of the fundamentals of fracture propagation processes, but also to clarify the limitations and applicability of simple criteria, e.g., T, COA or "final stretch" that have been derived under assumptions of J initiation criterion [52,53].

TABLE 10. BEHAVIOR OF CIRCUMFERENTIALLY FLAWED 6-INCH A106B SCHEDULE 80 PIPES UNDER BENDING AND PRESSURE STRESSES

Spec. No.	Flaw length, degrees	d/t	Rupture Pressure, ksi	Bending moment at Frupture, 10 in1b	Bending stress in outside fiber, ksi	Flaw Type
6-23-80	34.0	1.00	9.20	0	1	0.050 in. wide
6-27-8B	42.7	1.00	00.9	5.49	9.77	0.045 in. wide
6-25-80	0.89	1.00	8.20	0	1	0.050 in. wide
6-63-88	9.89	1.00	0	6.50	52.8	0.045 in. wide
6-20-80	360	0.28	6.79	0	1	0.020 in. wide
6-28-8B	360	0.30	6.52	09.9	53.6	0.020 in. wide
6-26-80	360	0.48	9.42	0	1	0.020 in. wide
6-64-8B	360	0.525	0	6.62	53.7	45° vee

1.82 1.02 2.00 1.14 1.08 1.32 17.58 17.12 1.59 0.28 17.67 0.62 17.31 3.17 8.47 2 17.56 0.196 0.61 22.98 6.45 0.82 1.00 87.0 1.00 19.0 0.122 0.193 0.268 0.352 0.205 0.301 Depth. Inch ; : Average Length, inches 19.85 20.08 26.59 1.85 3.69 Flav Date Length, degrees 360 360 35 360 360 89 180 Location Outside Outside Outside Outside Through Outside Through Outside Inside Burst Hoop Pressure Unflawed, Flawed, ksj(a) ksi 4.275 8.60 4.81 9.20 7.74 8.20 9.45 8.58 Tensile Data, Pressure Yield Ultimate, Elong, ksi ksi percent 8.78 8.75 9.20 8.80 8.82 5.63 Diameter, inches 6.46 99.9 99.9 99.9 6.68 9.66 99.9 6.67 Specimen Number Schedule 8-20-40 6-22-30 6-21-80 6-24-30 6-25-30 6-26-80 6-22-80 6-23-80 6-29-50 Well Thickness. inch 0.429 0.429 0.435 0.321 0.428 0.434 0.432 0.436 677.0

TABLE II. CIRCINGERENTIAL FLAW DATA ON A 106 B PIPE

Note: Elav Iype

a = 0.020-inch milled elot
b = 0.050-inch wide
c = 45 degrees Vee.

(a) Ultimate value used for Pb.

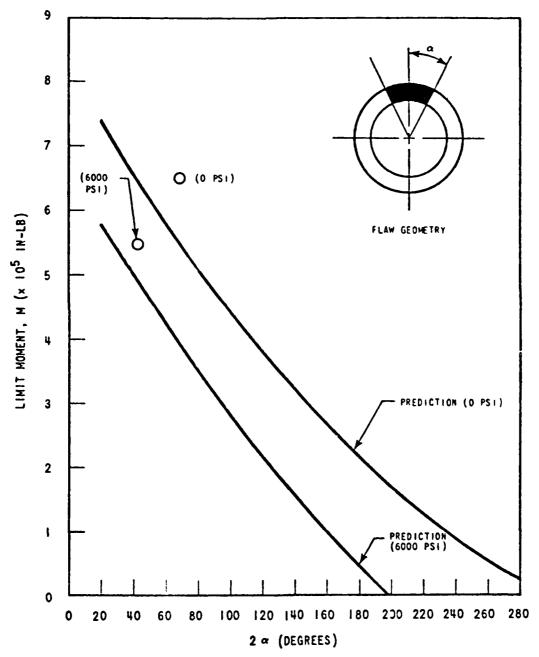


Fig. 29-Comparison of limit moment predictions with experimental results-A106B piping

3.4.1 Stable Crack Growth Criteria Based on the J-Controlled Growth

To treat elastic/plastic fracture initiation and propagation problems, crack opening displacement (COD), J controlled growth and energy method are candidates currently under intensive investigation. Although they have been proposed at different stages in the development of elastic/plastic fracture theory, there is strong correlation among them [47,48,49,50,51]. Because of the underlying assumption in these theories, extensive research effort is being carried on to establish the conditions under which they can be reliably utilized. To date, there is no single theory that can pass close scrutiny. However, provided certain requirements are satisfied, it is evident from the vast amount of available information that the J-controlled growth method can be employed as a useful tool to define structural stability against elastic/plastic fracture.

Following the introduction of the *J*-integral [7], J_{Ic} has been accepted as a elastic/plastic fracture initiation criterion [10,11,12,13] and the existence of a HRR (Hutchinson-Rice-Rosengren) field [8,9] has been identified as the necessary condition of a *J*-dominated stress field. In the *J*-integral derivation, it is assumed that no unloading occurs (deformation theory instead of incremental theory) and infinitesmal deformation (as opposed to finite strain) governs the kinematics relationship. Within the requirements of crack initiation, apparently both assumptions are acceptable. However, once the crack starts to propagate, further large deformation at the crack tip is expected and most of all, unloading is also experienced. Research efforts have been directed to extend *J* to a governing propagation parameter in spite of its underlying assumptions. Some efforts have been proven successful.

During crack growth there is some elastic unloading in the wake of advancing crack tip where the strains are strongly concentrated and where distinctly non-proportional plastic deformation occurs near the crack tip. Since the J-integral is theoretically based on the deformation theory of plasticity it does not adequately model any of these aspects of plastic behavior. Although, strictly speaking, J is restricted to the analysis of stationary cracks, a rationale is given by Hutchinson and Paris [53] for use of J

to analyze crack growth and stability under conditions which are called *J*-controlled growth. Assuming fully plastic situations for generally strain hardening materials, they considered the HRR (Hutchinson-Rice-Rosengren) type strain field based on the deformation theory for a growing crack, which is:

$$\epsilon_{ij} = K_n J^{\frac{n}{n+1}} r^{-\frac{n}{n+1}} \tilde{\epsilon}_{ij}(\theta)$$
 (16)

where,

 $K_n = a constant$

n = strain hardening coefficient

 r, θ = local polar coordinates at the current crack tip.

The strain increments under a simultaneous increase in J and crack length are written as

$$d\epsilon_{ij} = K_n J^{\frac{n}{n+1}} r^{-\frac{n}{n+1}} \left\{ \frac{n}{n+1} \frac{dJ}{J} \tilde{\epsilon}_{ij} + \frac{da}{r} \tilde{\beta}_{ij} \right\}$$
 (17)

where

$$\tilde{\beta}_{ij} = \frac{n}{n+1} \cos \theta \,\, \tilde{\epsilon}_{ij} + \sin \theta \,\, \frac{\partial}{\partial \theta} \, \tilde{\epsilon}_{ij} \tag{18}$$

da = increment of crack length, and Δa < < R.

Equation (17) indicates that the loading increments will be proportional $(d\epsilon_{ij} \sim \epsilon_{ii})$ if the first term dominates, which may be assured when

$$\frac{da}{r} < < \frac{dJ}{J}. ag{19}$$

If there exists an annular region

$$D < < r < R, \tag{20}$$

where

$$D = \left(\frac{dJ}{da} \frac{1}{J}\right)^{-1} \tag{21}$$

and R is a characteristic dimension for HRR field, then plastic loading is proportional and HRR singularity is dominant in this region. Therefore, deformation theory still remains as valid procedure for r > D and, the significance, for purpose of the present discussion, is that J uniquely measures or physically controls the fields specified by Eq. 20 for a growing crack. It may also be assumed that if predominantly proportional loading occurs throughout most of the singularity region, it will occur outside (r > R) this region as well [53]. Thus the requirements for the J-controlled growth are established.

If plane strain conditions are assumed to be present, which may be defined by the size requirement criterion,

$$Size \ge 25 J/\sigma_0, \tag{22}$$

the J-Resistance curve is size independent and may be reasonably configuration independent. Paris, et al. [54,59] proposed a Tearing Modulus to characterize a materials' stable tearing property,

$$T = \frac{E}{\sigma_0^2} \frac{dJ}{da} \tag{23}$$

where E is Young's modulus and a is the crack length. The behaviors of a structure during crack growth $(J_{app} > J_{l_c})$ is determined by the equilibrium condition

$$J_{\rm app} = J_{\rm mat}$$

and the stability criterion,

$$T_{\rm app} < T_{\rm mat} = {\rm stable}$$
 (24)
 $T_{\rm app} > T_{\rm mat} = {\rm unstable}$

where

$$T_{\text{mat}} = \frac{E}{\sigma_0^2} \frac{dJ_{\text{mat}}}{da} \tag{25}$$

The onset of instability holds when $T_{app} = T_{mat}$

For a bi-linear R-curve, dJ/da is simply the slope of the curve during crack extension; however, for arbitrary (non-linear) resistance curves, it should be noted that the Tearing Modulus (T) is dependent on the instantaneous J value.

Paris and his colleagues have demonstarated the applicability of the Tearing Instability Criterion for center cracked tension panels [56], HSST intermediate test vessels [56], and BWR pipe rupture test [55]. The effects of material strain hardening, small scale yield [54], and the correlation between tearing instability and Turner's η factor [57] have also been investigated. An experimental program utilizing three-point bend specimens was recently conducted and a good correlation between observed behavior and T-predicted instability response was noted [54].

Based on Rice's [60] J_2 flow theory for an ideally plastic material, similar studies have been conducted by Shih et. al. [61]. They considered the rate of change of the strain field crack growth in the form:

$$\frac{d\epsilon_{ij}}{da} = \frac{1}{r} \frac{d\delta}{da} f_{ij}(\theta) + \frac{\sigma_0}{E} \frac{1}{r} \ln \left(\frac{R(\theta)}{r} \right) g_{ij}(\theta)$$
 (26)

where

 δ = crack opening displacement

 $R(\theta)$ = a measure of the plastic zone size

 $\Delta a = \text{crack growth}; < < R$

 σ_0 = flow stress

E = Young's modulus

 $f_{ij}(\theta), g_{ij}(\theta) =$ dimensionless functions of order unity.

The first term in Eq. 26 represents the strain increment rate associated with crack tip blunting while the second term represents the strain increment rate caused by the crack advance. In Eq. 26, the strains at the crack tip may be characterized by the crack opening angle, $\frac{d\delta}{da}$, if the first term dominates that is,

$$\frac{d\delta}{da} > \frac{\sigma_0}{E} \ln \left(\frac{R(\theta)}{r} \right). \tag{27}$$

Therefore, Eq. 27 becomes the requirement for a crack opening angle-controlled crack growth. It should be noted that the strain fields, Eq. 21 and Eq. 26, derived from two different approaches, viz, J_2 deformation theory and J_2 flow theory, have a very similar structure. Therefore, if the HRR field grows more rapidly than the advancing crack, either $\frac{d\delta}{da}$ or $\frac{dJ}{da}$ may characterize the crack tip environment for a growing crack. Based on the crack opening angle, Shih, et al. [61], proposed a tearing modulus,

$$T_{\delta} = \frac{E}{\sigma_0} \frac{d\delta}{da} \tag{28}$$

as a parameter to characterize the stable crack growth and its stability. Extensive studies on verification of the validity of the crack opening angle to characterize crack growth have been done both experimentally and numerically by Shih, et al. [61], and Hahn, et al. [62].

Sorensen [50] and Rice and Sorensen [51] formulated a ductile crack growth criterion which describes the critical magnitude of a crack tip opening angle during the crack growth. They assumed a Prandtl slip-line stress field centered at a moving crack-tip in an elastic perfectly-plastic von Mises material. As a consequence of having the Prandtl field zone translate through the material with the advancing crack, they derived a crack tip opening angle during crack growth as,

$$\frac{\delta}{\Delta a} = \frac{\alpha}{\sigma_o} \frac{dJ}{da} + \beta \frac{\sigma_o}{E} \ln \left[\frac{eR}{\Delta a} \right]$$
 (29)

where

 $\sigma_o, E =$ as defined previously

R = plastic zone size; small scale yielding is assumed

 Δa = increments of crack extension; $\Delta a < < R$ is assumed

 δ = crack surface displacement at the previous crack tip

 α, β = constants.

If a stationary crack under monotonic loading is considered (i.e., $\Delta a = 0$), Eq. (29) integrates to the crack tip opening displacement,

$$\delta_{I} = \frac{\alpha}{\sigma_{o}} J. \tag{30}$$

The material dependent non-dimensional constant α correlates δ_t with J at the loading stage prior to the crack growth initiation. Another material constant β is theoretically defined as $\beta = 4 (2-\nu)/\sqrt{3}$, where ν is Poisson's ratio. However, the theoretical value of β may not accurately fit the relation for the results obtained numerically, because the discretized numerical procedure can not precisely simulate the continuous crack extension. As demonstrated by Sorensen [50], β can be reestimated from finite element solutions according to the following analysis.

Let the crack be incremented by Δa at a constant external load level so that the first term in the right hand side of Eq. (29) is zero. Assuming the plastic zone size, R, is proportional to EJ/σ_0^2 as is in the case of monotonic loading of a stationary crack, β may be estimated by

$$\frac{\delta}{\Delta a} \frac{E}{\sigma_o} = \beta \ln \left[\frac{\lambda eEJ}{\sigma_o^2 \Delta a} \right]$$
 (31)

where λ is a proportionality used for R, and may be fitted together with β .

Taking $\delta/\Delta a$ to be a material dependent constant during the crack growth, and assuming small scale yielding $(R = \lambda EJ/\sigma_o^2)$ Sorensen derived the following crack growth criterion from Eq. (29):

$$\frac{dJ}{da} = \frac{\beta}{\alpha} \frac{\sigma_o^2}{E} \ln \left(\frac{J_{ss}}{J} \right)$$
 (32)

where J_{ss} denotes J at steady state conditions $\frac{dJ}{da} = 0$, so that

$$J_{ss} = \frac{\sigma_o^2 \Delta a}{\lambda e E} \exp \left[\frac{E}{\beta \sigma_o} \frac{\delta}{\Delta a} \right]. \tag{33}$$

The criterion, Eq. (32), describes the J requirement necessary to continue stable crack growth. Equation (32) is integrated to obtain the current crack length as a function of the required J level, i.e.,

$$\frac{\sigma_o^2}{E} \frac{a - a_o}{J_{ss}} = \frac{\alpha}{\beta} \left[Ei \ln \left(\frac{J_{ss}}{J} \right) - Ei \ln \left(\frac{J_{ss}}{J_{lc}} \right) \right]$$
 (34)

where

$$Ei(x) = \int_{x}^{\infty} \frac{e^{-u}}{u} du$$
 (Exponential integral)

The crack growth criterion may be restated such that the necessary and sufficient condition to sustain crack extension is that the applied J equals the J required to meet the growth criterion (Eq. (34)), thus

$$J_A(Q,a) = J(a - a_a) \tag{35}$$

where Q denotes applied load. Likewise, instability will occur when applied value of dJ/da equals or exceeds the dJ/da required to meet the fracture criterion, thus

$$\frac{\partial J_A(Q,a)}{\partial a} \geqslant \frac{dJ(a-a_o)}{da}.$$
 (36)

Wnuk [63] also formulated an instability criterion for a growing crack based on the concept of final stretch, which is defined as an incremental displacement continually generated at the crack tip during the stable crack growth, linked with the Dugdale-Bilby-Cottrell-Swinden model. He obtained a

resistance curve for plastic zone size R and J for a cracked panel of infinite width that experienced a large scale yielding:

$$R = R_i \left[\frac{a}{a_o} \right]^{\lambda_i + 1} \exp \left[-\frac{1}{4} \ln^2 \left(\frac{a}{a_o} \right) \right]$$

OΓ

$$J = J_i \left(\frac{a}{a_o} \right) + \frac{8\sigma_y^2}{\pi E} a \left[\lambda_i ln \left(\frac{a}{a_o} \right) - \frac{1}{4} ln^2 \left(\frac{a}{a_o} \right) \right]$$
 (37)

where σ_y is yield strength and the subscript *i* implies the value of the parameters at the moment of crack growth initiation. The parameter λ measures the distance of any state during the stable crack growth from the ultimate loss of stability. Thus, it is called "stability index". At crack growth initiation, the index λ is defined as,

$$\lambda_{i} = \frac{\pi E}{8\sigma_{y}^{2}} \left[\left(\frac{dJ}{da} \right)_{i} - \left(\frac{\partial J_{A}}{\partial a} \right)_{i} \right]$$
 (38)

where $\frac{dJ}{da}$ is a measure of material resistance and the $\frac{\partial J_A}{\partial a}$ is an applied value. It is obvious that λ_i can be expressed in terms of tearing modulus T. Stable crack growth will occur if λ_i is greater than zero, and the crack will become unstable at the point where the λ drops to zero. However, for some types of cracked ductile specimens the crack may not grow to the critical size of instability. In such a case λ will never drop to zero and the specimen fails through a ductile tearing mechanism. Wnuk combined Eq. (37) with Eqs. (35) and (36) and derived the following expression for crack length at the terminal instability for a central crack panel:

$$a_f = a_o \exp \left[2\lambda_i\right]$$

$$a_f = \Delta a \exp \left[2(C-1)\right]$$
(39)

where

$$C = \frac{\delta}{\Delta a} \frac{\pi E}{8\sigma_{x}} - \frac{1}{2} \ln (2e)$$

where δ denotes the final stretch. The terminal toughness is given by

$$J_f = J_i e^{2\lambda_i} \left[1 + \frac{a_o}{J_i} \frac{8\sigma_Y^2}{\pi E} \lambda_i^2 \right]$$

or

$$J_f = \frac{J_i \Delta a}{a_o} e^{2(C-1)} \left\{ 1 + \frac{a_o}{J_i} \frac{8\sigma_Y^2}{\pi E} \left[(C-1)^2 - (C-1) ln \left(\frac{a_o}{\Delta a} \right) + \frac{1}{4} \ln^2 \left(\frac{a_o}{\Delta a} \right) \right] \right\}. \tag{40}$$

The advantage in these equations is that they can be used to predict the critical conditions in terms of known constants. It is interesting to note that similarities exist in the mathematical forms between the results obtained independently by Rice and Sorensen and by Wnuk. If Δa is assumed to be small compared to the plastic zone size R, Wnuk's equations can be modified and matched to those by Rice and Sorensen.

To summarize, although based on two different theories of plasticity, i.e., deformation theory and flow theory, the requirements of J-controlled crack growth and crack-tip opening displacement-controlled growth have been obtained by Hutchinson and Paris [54] and Shih et. al., [61] respectively. If these requirements are met, J and/or δ remain as valid tools to characterize stably growing cracks. Then Eqs. (24), (36), and (38), which are closely related to one another, give a fracture criterion in terms of tearing modulus T, J-resistance $\frac{dJ}{da}$, and stability index λ respectively. In addition, the instability condition is expressed in terms of terminal crack length by Eq. (39), and in terms of critical J value by Eq. (40).

3.4.2 Stable Crack Growth Criteria Based on the Griffith Energy Balance Equation

There exist other types of studies on stable crack growth whose associated failure criteria are not directly related to the *J*-controlled growth. Some of these are based on the Griffith energy balance concept extended to elastic-plastic materials undergoing slow crack growth in finite step sizes, Δa .

Neglecting dynamic and thermal effects on the structure, the energy balance for the structure during a step of crack advance may be written as

$$\frac{\Delta W_f}{\Delta a} = \frac{\Delta W_e + \Delta W_p + \Delta W_c}{\Delta a},\tag{41}$$

where

 ΔW_f = the external work increment applied to the structure

 ΔW_e = the elastic energy increment stored in the structure

 ΔW_p = the plastically dissipated energy increment in the structure

and

 ΔW_c = the work dissipated due to separation of the crack surface over Δa .

Postulating Δa is finite, define

$$G^* = \frac{\Delta W_f - \Delta W_e - \Delta W_p}{\Delta a} \tag{42}$$

and

$$G^{\Delta} = \frac{\Delta W_c}{\Delta a} \tag{43}$$

then G^* may be interpreted as the rate of energy available for creating new crack surfaces, and G^{Δ} is the rate of work required to quasi-statistically release the cohesive tractions holding the crack surfaces. During the process of stable crack growth, G^* and G^{Δ} are equivalent. Atluri, et. al., [64] and Hahn, et. al., [62] studied the G^* by finite element analysis which simulated a resistance curve from existing experimental data. On the other hand, the G^{Δ} has been studied by Hahn et. al., [62] and Kfouri and Miller [65]. As predicted by Rice [66] that at least for non-hardening materials, both G^* and G^{Δ}

reduce to zero as crack growth step size, Δa , tends to zero, this phenomenon was recognized even for a low hardening material by Atluri, et. al., [64] in their numerical analyses. They discussed that Δa in finite element analyses of stable crack growth must by selected four to five times crack opening displacement at incipient growth condition to obtain meaningful results of G^* or G^{Δ} .

There may exist a small region ahead of a growing crack-tip in which some non-linear irreversible process occurs. This region is called a "crack-tip process zone." The rate of energy dissipated due to the irreversible process in the process zone can be thought as a material property. Denoting this energy dissipation rate by G_{pz} , the energy flow rate into the process zone, G^*_{pz} is equated to the sum of G^{Δ} and G_{pz} , i.e.,

$$G_{pz}^{\bullet} = G^{\Delta} + G_{pz}. \tag{44}$$

This energy flow rate, G_{pz}^{\bullet} , can be obtained by numerically evaluating change of the energy over the entire structure excluding the process zone, thus

$$G_{pz}^{\bullet} = \frac{\Delta W_f}{\Delta a} - \frac{\left[\Delta W_e + \Delta W_p\right]_{\Omega - p}}{\Delta a} \tag{45}$$

or equivalently

$$G_{pz}^{\bullet} = \int_{\partial \Gamma} T_i \, \frac{\Delta \, U_i}{\Delta \, a} \, ds \tag{46}$$

where T_i are the tractions at the boundary $\partial \Gamma$ of the process zone Γ , ΔU_i are increments of displacements on $\partial \Gamma$, and $[]_{\Omega-p}$ in Eq. (45) denotes that the quantities in [] are integrated in the rest of the structure excluding the process zone. G_{pz}^{\bullet} has been studied by Hahn et. al., [62] and Atluri et. al., [64]. The size of the process zone recommended by Hahn, et. al., is to be taken on the order of plate thickness, and maybe smaller for the plane strain case.

Another candidate for a criterion to characterize stable crack growth and possibly predict the onset of fracture is a crack tip nodal force. This has been proposed and studied by Hahn, et. al., [62]. Although this is intuitively appealing, the theoretical basis for use of the crack tip nodal force has not yet been established.

4.0 LEAK BEFORE BREAK CRITERIA

It is very desirable that pipe rupture is preceded by leakage so that necessary measures can be undertaken to remedy the situation. Therefore, there are two aspects to be considered: (1) the possibility of leak before break, and (2) the acceptable leakage rate. The state of art of pipe rupture in the elastic/plastic region is only at the semi-empirical stage. Therefore, effort has been devoted to the definition of critical crack length with only little emphasis to the mouth opening, which is one of the means to measure leakage rate.

For pipes fabricated from austenitic stainless steel or ferritic steels (at shelf temperature), pipe fracture is unlikely to occur unless the structure has reached its limit load capability. In that case, ductile tearing is the failure mode. From all the experimental and analytical results reviewed, the crack length that corresponds to limit load (flow stress criterion) is generally very large and excessive leakage would have been developed well before crack of such length is developed [3, 29].

For pipes fabricated from ferritic steels that operate in the transition temperature region, mixed mode failure consisting of brittle fracture and ductile tearing is observed. The leakage rate is determined by the degree of mouth opening. Analytically, the crack opening can be approximated as the sums of elastic displacement, plastic correction and bulging to pipe geometry. The following derivation is from Ref. 29.

$$A = \text{Mouth opening area} = A_1 \text{ (Elastic)} + A_2 \text{ (Plastic)} + A_3 \text{ (Bulging)},$$

$$\text{where } A_1 = \frac{2(1 - v^2)}{E} \cdot \sqrt{\frac{c}{\pi}} K\pi c$$

$$A_2 = \frac{4\sigma_y c^2}{E} \ln \text{Sec} \left[\frac{\pi}{2} \frac{\sigma}{\sigma_y} \right].$$

and

$$A_3 = \frac{2\pi}{3} y_o c (2y_0/R)^{1/2};$$

in which,

2c = crack length

ν = Poisson's Ratio

E = Modulus

 σ_y = yield strength

 σ = applied stress

 y_0 = amount of bulging (Ref. 29)

K = stress intensity factor

R = pipe radius

5.0 CONCLUSIONS

An extensive literature review concerning experimental data and predictive capability of elastic/plastic pipe rupture has been completed. The materials used for nuclear reactor piping can be classified as high toughness and medium to high toughness materials. High toughness material, including austenitic stainless steel, exhibits no brittle to ductile transition temperature and ductile tearing is

the failure mode. Medium to high toughness materials, including ferritic steels, SA 106, SA 333 and SA 561, exhibit high ductility at the shelf temperature and fail in a mixed (brittle/ductile) fracture mode in the transition temperature region.

The predictive tools reviewed are classified into three major categories; the overall structural response computation, the semi-empirical method, and rigorous elastic/plastic fracture mechanics. Lack of adequate elastic/plastic fracture criteria and excessive computational expense limit the applicability of overall structural response computation. For the cases studied, the flow stress theory, which assumes pipe rupture from limit load, is adequate to predict failure of high toughness materials and medium to high toughness materials at the shelf temperature. The pseudo-toughness approach, K_c , has been used to describe pipe failure in the transition temperature region with limited success. Therefore, for those materials which operate in the transition region, the real solution is to ultilize rigorous elastic/plastic fracture mechanics methodology. Among the current theoretical developments in the analysis of advancing cracks, the *J*-controlled growth methods are one of the most promising and most widely accepted. All the criteria proposed to data, i.e., Tearing Modulus, COA, final stretch, and Stability Index, are capable of describing a small amount of crack growth and they are all mathematically related. To permit quantitative assessment of safety factors, *J*-integral resistance curves of current nuclear piping materials should be generated.

The high fracture toughness levels associated with existing nuclear piping configurations and materials suggests that extensive plastic deformation will precede failure. No sudden (catastrophic) ruptures are expected and a favorable leak-before-break condition should prevail. The mouth opening on the pipes of these materials in the transition region can be approximated by linear elastic mechanics modified by plasticity and geometry corrections.

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Appendix A
LIST OF EXPERIMENTAL DATA
From Ref. 26

TABLE
Summay of flat-plate crack-extension measurements performed by Kihara et al. on
19.7-in.-long by 15.7-in.-wide hot-rolled steel plates with 3.14-in.-long edge cracks.

Plate thickness, in.	Test temp, C	σ•, psi	K _c , ksi √in. ^(a)
0.25	-118	20,300	73
	-138	18,000	65
	-158	14,500	52
	-170	15,600	56
	– 196	8,170	29
0.375	-118	25,200	90
	-138	20,200	73
	-158	15,600	56
	. – 180	12,400	45
0.500	118	28,400	100
	- 138	23,800	85
	-158	17,000	61
	180	9,900	36

^(a) $K_c = 1.14 \ \sigma^*(\pi c)^{\frac{1}{2}}$, no plasticity correction was necessary since $\sigma^*/\sigma_{\gamma} < 0.4$ in all cases.

Compilations of pressure-vessel test data

TABLE

Data summary for Anderson and Sullivan for aluminum-alloy vessels

Material properties			Vessel	geometr	,	Test conditions	•		Calcul	ated values	-
Designation	σ _γ , ksi	σ _υ , ksi	R, in.	t, in.	R/t	Temp, C	c, in.	σ _k , ksi	c²/Rt	φ,	$(\sigma_H^{\bullet 2}\pi c \varphi_j)^{-1} \times 10^{-10} (in.^3) (lb.^{-2})$
Aluminum 2014-T6	68	79	2.81	0.06	46.8	Room Temp.	0.06	64.4	0.02	2.42/1.55	5.29/ 8.26
Ditto	68	79	2.81	0.06	46.8	Ditto	0.25	34.0	0.37	1.2 /1.14	9.17/ 9.66
Ditto	68	79	2.81	0.06	46.8	Ditto	0.50	20.6	1.48	1.13/1.09	13.40/13.76
Ditto	68	79	2.81	0.06	46.8	Ditto	1.00	9.7	5.93	1.08/1.06	31.32/31.91
Ditto	68	79	2.81	0.06	46.8	- 196	0.05	71.6	0.014	1.75/1.42	7.09/ 8.74
Ditto	82	93.9	2.81	0.06	46.8	- 196	0.07	70.6	0.029	1.74/1.41	5.24/ 6.47
Ditto	82	93.9	2.81	0.06	46.8	1 96	0.10	63.7	0.059	1.49/1.31	5.26/ 5.98
Ditto	82	93.9	2.81	0.06	46.8	1 96	0.12	58.5	0.085	1.39/1.26	5.57/ 6.15
Ditto	82	93.9	2.81	0.06	46.8	- 19 6	0.15	52.2	0.13	1.29/1.20	6.03/ 6.49
Ditto	82	93.9	2.81	0.06	46.8	196	0.20	47.4	0.23	1.25/1.17	5.66/ 6.03
Ditto	82	93.9	2.81	0.06	46.8	- 196	0.25	40.1	0.37	1.19/1.13	6.65/ 7.00
Ditto	82	93.9	2.81	0.06	46.8	- 196	0.37	30.2	0.81	1.14/1.10	8.27/ 8.57
Ditto	82	93.9	2.81	0.06	46.8	- 19 6	0.50	23.1	1.48	1.11/1.08	10.75/11.04
Ditto	82	93.9	2.81	0.06	46.8	– 196	0.62	18.6	2.28	1.09/1.07	13.61/13.86
Ditto	82	93.9	2.81	0.06	46.8	- 196	0.87	14.4	4.50	1.09/1.07	16.10/16.48
Ditto	82	93.9	2.81	0.06	46.8	- 196	1.00	11.3	5.80	1.07/1.05	23.30/23.68
Ditto	90.5	93.9	2.81	0.06	46.8	- 253	0.05	82.2	0.014	1.97/1.77	4.78/ 5.32
Ditto	90.5	93.9	2.81	0.06	46.8	- 253	0.12	63.4	0.08	1.38/1.34	4.78/ 4.92
Diito	90.5	93.9	2.81	0.06	46.8	- 253	0.25	39.6	0.37	1.16/1.14	6.99/ 7.12
Ditto	90.5	93.9	2.81	0.06	46.8	- 253	0.37	32.0	0.81	1.15/1.14	7.30/ 7.37
Ditto	90 5	93.9	2.81	0.06	46.8	- 253	0 50	21.0	1.48	1.08/1.08	13.36/13.38
Ditto	90 5	93.9	2.81	0.06	46.8	253	0.63	198	2.35	1.11/1.10	11.60/11.70
Ditto	90.5	93.9	2.81	0.06	46.8	- 253	0.87	13.2	4.52	1.08/1.07	19.45/19.63
Ditto	90.5	93.9	2.81	0.06	46.8	 253	1.00	11.9	5.93	1.08/1.08	20.80/20.80

^(a) Two values are computed for φ_3 and $\sigma_H^{*2}\pi c \varphi_3$ corresponding to the upper and lower bounds for $\hat{\sigma}: \hat{\sigma} = \sigma_0$.

TABLE Data summary for Getz, Pierce, and Calvet , or aluminum-alloy vessels

Material properties			Vessel	gcometr	y	Test condi	tions		Calcul	ated values"	•
Designation	σ _P , ksi	σ _ε , ksi	R, in.	L in.	R/t	Temp, C	c, in.	ση, ksi	c²/Rt	φ,	$(\sigma_H^{*2}\pi c \varphi_3)^{-1} \times 10^{-10} (in.^3) (lb.^{-2})$
Aluminum 2014-T6	90.5	93.9	3.0	0.06	50	- 253	0.05	81	0.013	1.86/1.70	5.21/ 5.71
Ditto	90.5	93.9	3.0	0.06	50	- 253	0.05	83	0.013	1.97/1.80	4.70/ 5.14
Ditto	9.05	93. 9	3.0	0.06	50	- 253	0.05	86	0.013	2.54/2.05	3.39/ 4.20
Ditto	9.05	93.9	3.0	0.06	50	- 253	0.07	73	0.027	1.53/1.46	5.57/ 5 84
Ditto	90.5	93.9	3.0	0.06	50	- 253	0.12	63	0.08	1.36/1.31	4.91/ 5.10
Ditto	90.5	93.9	3.0	0.06	50	- 253	0.25	40	0.34	1.14/1.13	6.98/ 7.04
Ditto	90.5	93.9	3.0	0.06	50	-253	0.25	39	0.34	1.13/1.12	7.41/ 7.47
Ditto	90.5	93.9	3.0	0.06	50	- 253	0.37	33	0.76	1.12/1.11	7.05/ 7.18
Ditto	90.5	93.9	3.0	0.06	50	253	0.50	21	1.38	1.06/1.06	13.63/13.63
Ditto	90.5	93.9	3.0	0.06	50	-253	0.61	20	2.06	1.08/1.07	12.08/12.20
Ditto	90.5	93.9	3.0	0.06	50	- 253	0.87	14	4.20	1.06/1.06	17.63/17.63
Ditto	90.5	93.9	3.0	0.06	50	- 253	1.0	11	5.50	1.05/1.04	25.06/25.18
Ditto	90.5	93.9	3.0	0.06	50	- 253	1.0	13	5.50	1.07/1.06	17.63/17.79
Ditto	82.0	93.9	3.0	0.06	50	- 1 96	0.06	70	0.02	1.65/1.40	6.5 / 7.7
Ditto	82.0	93.9	3.0	0.06	50	19 6	0.06	72	0.02	1.80/1.45	5.69/ 7.06
Ditto	82.0	93. 9	3.0	0.06	50	- 1 96	0.06	75	0.02	2.10/1.50	4.49/ 6.29
Ditto	62.0	93.9	3.0	0.06	50	- 196	0.07	72	0.027	1.90/1.45	4.62/ 6.05
Ditto	82.0	93.9	3.0	0.06	50	19 6	0.10	65	0.055	1.50/1.35	5.02/ 5.58
Ditto	82.0	93.9	3.0	0.06	50	- 196	0.14	60	0.10	1.40/1.30	4.51/ 4.86
Ditto	82.0	93.9	3.0	0.06	50	196	0.15	54	0.12	1.35/1.20	5.39/ 6.06
Ditto	82.0	93.9	3.0	0.06	50	- 196	0.20	45	0.22	1.20/1.15	6.55/ 6.54
Ditto	82.0	93.9	3.0	0.06	50 `	- 196	0.20	50	0.22	1.30/1.20	4.89, 5.30
Ditto	82.0	93.9	3.0	0.06	50	- 196	0.25	39	0.34	1.20 1.10	6.98/ 7.62
Ditto	82.0	93.9	3.0	0.06	50	- 196	0.25	41	0.34	1.20, 1.10	6.31/ 6.89
Ditto	82.0	93.9	3.0	0.06	50	196	0.37	30	0.76	1.10 1.10	8.69/ 8.69
Ditto	82.0	93.9	3.0	0.06	50	- 196	0.50	23	1.38	1.10/1.07	10.95, 11.26
Ditto	82.0	93.9	3.0	0.06	50	- 196	1.00	20	5.50	1.05 1.04	30.33, 30.60
Ditto	82.0	93.9	3.0	0.06	50	- 196	1.00	11	5.50	1.06.1 04	24.89/25.37

⁽a) Two values are computed for φ_3 and $\sigma_{gl}^{*2}\pi c \varphi_3$ corresponding to the upper and lower bounds for $\hat{\sigma} : \hat{\sigma} = \sigma_{\gamma}, \hat{\sigma} = \sigma_{\xi}$.

TABLE Data summary for Duffy et al. for ductile crack extension in steel pipes

Material properties	•		Vessel	geometry		Test condi	ions		Calcula	ited values	•1	
Designation ^(b)	σ _γ , ksi	συ, ksi	R, in.	c, in.	R/t	Temp, C	c. in	σů, ksi	c ¹ .Rt	φ ₃	$(\sigma_H^{0.2}\pi c \omega_3)^{-1} \times 10^{-10} (\text{in.}^3) (1b^{-2})$	σ ⁴⁻² × 10 ⁻¹⁰ (in ⁴) (1b. ⁻²)
Steel RR, TR, BB	60	80	15	0.375	40	-20-24	0.5	70.6	0.044	∝,200	0,0.638	2.00
Ditto	60	80	15	0.375	40	- 20-24	0.5	69.8	0.044	x /2.00	0/0.654	2.05
Ditto	60	80	15	0.375	40	- 20-24	1.65	56.2	0.483	x/1.85	0/0.331	3.16
Ditto	60	80	15	0.375	40	- 20-24	1.65	55.8	0.483	x/1.85	0/0.335	3.20
Ditto	60	80	15	0.375	40	- 20-24	2.25	46.B	0.90	x/1.70	0/0.380	4.50
Ditto	60	80	15	9.375	40	- 20-24	2.70	42.6	1.30	≭/1.85	0,0.351	5.50
Ditto	60	60	15	0.375	40	-20-24	3.20	38.8	1.82	x/20	0/0.329	6.64
Ditto	60	80	15	0.375	40	- 20-24	4.40	28.2	3.34	∝/1.60	0/0.569	12.50
Ditto	60	80	15	0.375	40	- 20-24	4.40	27.8	3.34	∝/1.55	0/0.604	12.90
Ditto	60	60	15	0.375	40	- 20-24	4.40	27.6	3.34	x/1.55	0/0.613	13.10
Ditto	60	80	15	0.375	40	- 20-24	4.40	27.6	3.34	x/1.55	0/0.613	13.10
Steel AF	68	84	15	0.375	40	16-16	2.65	48.7	1.25	∝ /2.20	0/0.230	4.22
Ditto	68	84	15	0.375	40	- 16-16	2.65	48.1	1.25	∝/2.10	0/0.247	4.32
Ditto	68	84	15	0.375	40	- 16-16	2.65	47.4	1.25	x/1.90	0/0.281	4 45
Ditto	68	84	15	0.375	40	- 16-16	4.40	31.6	3.34	∝/1.75	0/0.414	10.00
Ditto	68	84	15	0.375	40	- 16-16	7.50	16.5	10.0	1.9 /1.35	0.82 /1.156	37.20
Ditto	68	84	15	0.375	40	- 16-16	10.00	11.4	17.6	1.59/1.25	1.54 /1.96	76.90
Steel AC, AD	53	75	15	0.375	40	2-23	3.5	33.0	2.18	ox /1.65	0/0.506	9.18
Ditto	53	75	15	0.375	40	2-23	3.5	32.8	2.18	⊄/1.65	0/0.512	9.30
Ditto	53	75	15	0.375	40	2-23	3.5	32.4	2.18	⊄ /1.62	0/0.535	9.53
Steel UU	61.7	70	3.06	0.25	12.25	- 2-0	2.20	25.3	6.35	α(x	0	15.60
Ditto	61.7	70	3.06	0.25	12.25	- 2-0	3.55	15.3	16.4	or/x	0	42.70
Steel GP	51	73	13	0.281	46.4	17	2.55	37.9	1.78	ar/ac	0	6.90
Steel AH	60	80	18	0.406	45	-84	2.7	43.9	1.0	x/1.55	0/0.394	5.10
Ditto	60	80	16	0.406	45	- 8 4	2.7	44.7	10	x /1.57	0/0.376	5.00
Ditto	60	80	16	0.406	45	- 8 4	2.7	46.0	1.0	x/165	0/0.337	4.70
Steel YY	62	74	18	0.861	21	62	4.85	33.6	1.50	26,15	0 223/0 387	8.80

⁽⁶⁾ Two values are computed for φ_1 and σ_0^2 $\pi c \varphi_2$ corresponding to the upper and lower bounds for $\hat{\sigma}: \hat{\sigma}: \hat{\sigma}_1, \hat{\sigma} = \sigma_0$.
⁽⁶⁾ The steels employed in this study are X-50 and X-60 grade line-pipe steels.

TABLE Data summary for Nichols et al. for ductile and semibrittle crack extension in steel, pressure cessels

Material properti	es		Vessel	geometr	y	Test cond	itions		Calcul	ated values	a 1	
Designation	σ _γ , ksi	σ _t , ksi	R, in.	r, in.	R/t	Temp, C	c, in	σĝ, ksi	c²/Rt	Ψ,		σ° 2 χ 10 - 10 (ιπ.4 (lb 2)
0.36 C Steel ^(b)	34.5	69.5	30	1.0	30	1-51	3	27.6	0.3	2.3 /1.12	0.6 /1.24	
Ditto	34.5	69.5	30	1.0	30	1-51	3	32.2	0.3	∝/1.16	0/0.88	
Ditto	34 5	69.5	30	1.0	30	1~51	6	18.8	1.2	1.8 /1.09	0.83/1.37	
Ditto	34.5	69.5	30	1.0	30	1-51	6	17.9	1.2	1.62/1 08	1.02/1.53	
Ditto	34.5	69.5	30	1.0	30	1-51	6	21.0	1.2	∝/1.12	0/1.07	
Ditto	34.5	69.5	30	1.0	30	1-51	6	15.9	1.2	1.4 /1.06	1.49/1.98	
Ditto	34.5	69.5	30	1.0	30	1-51	12.37	9.6	5.0	1 5 /1.07	1.86/2.61	
Ditto	34.5	69.5	30	1.0	30	62-88	3	33.0	0.3			9.8
Ditto	34.5	69.5	30	1.0	30	62-88	6	25.7	1.2	_		15.0
Ditto	34.5	69.5	30	1.0	30	62-88	6	27.7	1.2	_	-	13.0
Ditto	34.5	69.5	30	1.0	30	62-88	12	12.7	4.8		_	62.0
Ditto	34.5	69.5	30	1.0	30	62-88	12	15.2	4.8			43.28
Ditto	34.5	69.5	18	1.0	18	10-50	6	13.9	2.0	1.4 /1.06	1.96/2.59	
Ditto	34.5	69.5	18	1.0	18	10-50	6	17.4	2.0	2.15/1.08	0.81/1.62	
D:tto	34.5	69.5	18	1.0	18	79	6	23.4	2.0	_	_	18.2
D:tto	34.5	69.5	57	1.0	57	17	6	22.0	0.63	1.55/1.07	0.7 /1.02	
Ditto	34.5	69.5	57	1.0	57	80	6	27.2	0.63		_	13.5
0.13 C Steel(s)	40.0	63.5	30	10	30	16-79	6	29.9	1.2	_	_	11.1
Ditto	40.0	63.5	30	1.0	30	16-79	6	31.8	1.2	_	_	9.88
Ditto	40.0	63.5	30	1.0	30	16-79	6	29.4	1.2	-	-	11.56
Ditto	40.0	63.5	30	1.0	30	16-79	6	31.8	1.2	-	_	9.88
Ditto	40.0	63.5	30	1.0	30	16-79	12	19.5	4.8	_		26.2
0.16 C Steelter	31.0	64.0	30	1.0	30	39	6	28.5	1.2	_		13.5

TABLE Data summary for Kihara, Ikeda, and Iwanga for brittle-steel vessels

Material prop	erties		Vessel g	reometry		Test condit	ions		Calcula	ted valu	8
Designation	σ _F , ksi	σ_C , ksi	R, in.	t, in.	R/t	Temp, C	c, in.	σ², ksi	c²/Rt	₹3	$(\sigma_H^{0.2}\pi c \varphi_3)^{-1} \times 10^{-10} (in.^3) (lb.^{-2})$
Steel'*	115	125	4.3	0.25	17	- 196	2.44	3.98	5.56	1.00	82.64
Ditto	115	125	4.3	0.25	17	- 196	1.96	4.95	3.59	1.00	66.22
Ditto	115	125	4.3	0.25	17	- 196	1.35	8.25	1.70	1.00	34.6
Ditto	115	125	4.3	0.25	17	– 196	0.86	13.2	0.69	1.00	21.17
Ditto	115	125	8.0	0.25	32	196	3.22	4.95	5.18	1.00	40.48
Ditto	115	125	8.0	0.25	32	196	2.53	5.60	3.20	1.00	40.16
Ditto	115	125	8.0	0.25	32	- 196	1.85	8.52	1.71	1.00	23.69
Ditto	115	125	8.0	0.25	32	- 196	1.16	9.60	0.67	1.00	29.76
Ditto	115	125	6.0	0.25	25	- 1 96	1.65	7.56	1.80	1.00	33.78
Ditto	115	125	6.4	0.375	17	196	2.0	4.40	1.66	1.00	81.96
Ditto	115	125	6.4	0.375	17	196	2.0	5.70	1.66	1.00	49.01
Ditto	115	125	4.3	0.375	11.4	- 196	1.65	7.40	1.68	1.00	35.21
Ditto	115	125	8.0	0.375	21.3	- 196	2.24	9.90	1.67	1.00	14.42
Ditto	115	125	4.3	0.50	8.6	- 196	2.30	3.42	5.44	1.00	176.0
Ditto	115	125	4.3	0.50	8.6	- 196	2.63	3.50	3.20	1.00	99.0
Ditto	115	125	4.3	0.50	8.6	- 19 6	1.94	4.20	1.75	1.00	92.59
Ditto	115	125	4.3	0.50	8.6	- 196	1.16	9.20	0.62	1.00	32.46
Ditto	115	125	8.0	0.50	16	- 196	3.62	2.40	3.27	1.00	153.8
Ditto	115	125	8.0	0.50	16	- 196	2.53	4.80	1.60	1.00	54.64
Ditto	115	125	8.0	0.50	16	196	1.55	7.20	0.60	1.00	39.58
Ditto	115	125	6.4	0.50	12.8	196	2.34	4.90	1.71	1.00	56.49

⁽e) Hot-Rolled Steel; C: 0.25%, Si: 0.02%, Ma: 0.85%.

[&]quot;Two values are computed for φ_1 and $\sigma_R^{(2)}\pi c \varphi_2$ corresponding to the upper and lower bounds for $\tilde{\sigma}: \tilde{\sigma} = \sigma_T, \tilde{\sigma} = \sigma_U$.

Plain carbon steel; C:0.36%, Mn :0.44-0.46%, Si: 0.10-0.13%, The mode of crack extension in this steel was 100 percent ductile shear above 51 C, semi-

brittle below 51 C.

*** Aluminum grain-refined steel; C: 0.13° ,... Mn: 1.14° ;. Si: 0.12° ... Crack extension mode was 100 percent ductile shear in all cases.

*** Sincon-xilled steel; C: 0.16° ;... Mn: 1.22° ,... Si: 0.20° ... Crack extension mode was 100 percent ductile shear in all cases.

TABLE

Data summary	for Almon	d et ul.	for ductile-	steel tesse	ls								
Material prop	erties		Vessel (geometry		Test condi	Test conditions C			Calculated values			
Designation	σ ₁ , ksi	σ _υ , ksi	R, ia.	t, in.	R,T	Temp, C	c, in.	σů, ksi	c²/Ri	φ,	$(\sigma_H^{*2}\pi c \varphi_3)^{-1} \times 10^{-10} (\text{in.}^3) (\text{lb.}^{-2})$	c* · 2 x 10 · 10 (in.4)(lb.2)	
Steeliei	45.7	66.0	2.5	0.5	5.0	-25	1.125	32.0	1.01	_		9.75	
Ditto	45.7	66.0	2.5	0.5	5.0	25	1.125	35.5	101			7.94	
Ditto	45.7	66.0	2.5	0.5	5.0	- 25	1.125	36.0	1.01			7.70	
Ditte	47.0	70.6	2.5	0.5	5.0	5-5	1.125	38.0	1.01			6.94	
Ditto	47.0	70.6	2.5	0.5	5.0	-5-5	1.125	36.5	1.01	_	-	7.50	
Ditto	47.0	70.6	2.5	0.5	5.0	- 5-5	1.125	35.5	1.01			7.94	
Ditto	49	77	2.5	0.5	5.0	- 68	1.125	42.5	1.01	-		5.54	
Ditto	66	88	2.5	0.5	5.0	- 120	1.125	45.7	1.01			4.80	

Hot Rolled Steel; C: 0.14%, Si: 0.26%, Ma: 0.47%. Crack extension occurred by ductile fibrous mode, at least initially.

TABLE

Material properties			Vessel	geometr	i	Test condition	ns		Calculated valu	es	
Designation	σ _γ , k si	σ _υ , ksi	R, ia.	t, in.	R/t	Temp. C	c, in.	σ _H , ksı	50(c ² , R ²)tanh (R; 50t)	Ψ,	$(\sigma_N^{\bullet 2} \pi c \varphi_3)^{-1} \times 10^{-10} (\text{in.}^3) (\text{ib.}^{-2})$
Aluminum 2024-T3	36.5	65.0	14.4	0.015	960	Room Temp	0.31	41.3	0.023	x/1.25	0. 4.81
Ditto	36.5	65.0	14.4	0 0 1 5	960	Ditto	0.64	29 8	0 (198	1.74 1.12	3.21 4.99
Ditto	36.5	65.0	14.4	0.015	960	Ditto	1.25	20.4	0.37	13:107	4 67, 571
Ditto	36.5	65.0	14.4	0.015	960	Ditto	2.55	11.3	1.56	1.18 1 04	8.28 9.39
Ditto	36.5	65.0	14.4	0.015	960	Ditto	3.85	8.2	3.57	1 18, 1 05	10.42, 11.71
Ditto	36.5	65.0	3.6	0.025	144	Ditto	0 50	21.9	0.96	2.62, 1.15	5 06 11.54
Ditto	36.5	65.0	3.6	0.025	144	Ditto	1.0	10.4	3 \$4	1.41, 1.08	20.85 27.23
Ditto	36.5	65.0	3.6	0.025	144	Ditto	2 81	3.4	29 50	1.25, 1.06	78.43 92 48
Ditto	36.5	65.0	3.6	0.015	230	Ditto	0.31	29.3	0.37	x 1.18	0 10 13
Ditto	36.5	65.0	3.6	0.015	230	Ditto	0.60	17.2	1 38	16 /111	11 20 16 14
Ditto	36.5	65.0	3.6	0.015	230	Ditto	1 20	8 7	5.50	1.39, 1.08	25 24 32 48
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0.49	22.9	0 92	x/1.16	0 10 68
Ditto	36.5	65.0	3.6	0.012	300	Ditto	1.0	12.8	3 85	2.18 i 14	8 90, 17.03
Ditto	36.5	65.0	3.6	0.012	300	Ditto	20	5.7	15.40	1 46 1.09	33.57.44.97
Ditto	36.5	65.0	3.6	0.012	300	Ditto	1.90	5.4	13 90	1.32 1.07	43 53 53.7
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0.48	22.8	0.88	2.62 1.15	4 86 11 09
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0.95	10.2	3.48	1.34 1.07	23.99 30 05
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0.28	40.2	0.05	oc/1.24	0. 5.67
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0 12	41.4	0.05	x,1.26	0.12.28
Ditto	36.5	65.0	3.6	0.012	300	Ditto	√25	30.6	0.25	x 1.16	0,11.72
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0.25	26.4	0.25	1.41,7.11	12.96 16.46
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0.48	20.0	0.80	1.57/1.10	10.56, 15.07
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0.93	10.7	3 35	1.37.1.08	21.78 27 63
Ditto	36.5	65.0	3.6	0.012	300	Ditto	1.91	4.9	12.50	1.22/1 66	56.42 65.51
Ditto	36.5	65.0	3.6	0.012	300	Ditto	3.80	2.6	50.0	1.24/1.66	99.56:116.46
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0.48	20.4	0.80	1.62/1.11	9.82 14.34
Ditto	36.5	65.0	3.6	0.012	300	Ditto	0.48	21.0	0.80	1.71/1.12	8.79/13.42
Ditto	36.5	65.0	3.6	0.06	680	Ditto	0.12	44.4	0.05	∝/1.32	0, 10.39
Ditto	36.5	65.0	3.6	0.06	600	Ditto	0.23	27.3	0.15	1.56/1.10	11.89 16.86
Ditto	36.5	65.0	3.6	0.06	600	Ditto	0.48	20.7	0.80	1.67/1.11	9.26, 13.94
Ditto	36.5	65.0	3.6	0.06	600	Ditto	0.98	10.2	3.50	1.34/1.07	23.32/29.2

TABLE

Data summary for Peters and Kuhn for aluminum-alloy vessels

Materials properties					Vessel geometry				Calculated values ^(a)		
Designation	ø _y , ksi	σ _U , ksi	R, in.	r, in.	Rt	Temp, C	c, in.	σĝ, ksi	50(c ² /R ²) tanh (R/50t)	φ,	$(\sigma_H^{0.2} \pi c \varphi_3)^{-1} \times 10^{-10} (in.^3) (lb.^{-2})$
Aluminum 7075-T6	65	80	3.6	0.016	225	Room Temp	0.33	19.4	0.40	1.06/1.04	24.68/ 24.65
Ditto	65	60	3.6	0.016	225	Ditto	0.65	11.7	1 60	1.05/1.03	34.08; 34.74
Ditto	65	80	3.6	0.016	225	Ditto	1.28	5.5	4.50	1 02 1.01	80.60/ 81.43
Ditto	65	80	3.6	0.025	144	Ditto	0.50	16.6	0.50	1.05/1.03	22.01 - 22.44
Dino	65	80	3.6	0.025	144	Ditto	1.0	8.4	3.90	1 06/1.03	42.57/ 43.81
Ditto	65	80	3.6	0.025	144	Ditto	2.0	3.7	15.50	1.04, 1.02	111.84:114.03
Ditto	65	80	14.4	0.016	960	Ditto	0.31	37.2	0.02	2 02/1.39	3.67/ 5.34
Ditto	65	80	14.4	0.016	960	Ditto	065	24.9	0.09	1.08/1.05	7.31/ 7.52
Ditto	65	80	14.4	0.017	847	Ditto	1 30	136	0.40	1.03, 1.02	12.85/ 12.98
Ditto	65	80	14.4	0.017	847	Ditto	2.50	8.5	1.40	1.02/1.01	17 29/ 17.46

Two values are computed for φ_3 and $\sigma_0^{2,2}$ acceptances on the upper and lower bounds for $\hat{\sigma}: \hat{\sigma} = \sigma_1, \hat{\sigma} = \sigma_U$.

TABLE

Data summary for				ium-allo	y cessels							
Material propertie	5		Vessel	geometr	y ^{ta)}	Test conditio	ns		Calculated values ^(b)			
Designation	σ _τ , ksi	σ _υ , ksi	R, in.	e, in.	R/t	Temp, C	c, in.	σů, ksi	50(c²/R²) tanh (R'50r)	φ,	(σ ² ² πεφ ₃) ⁻¹ κ 10 ⁻¹⁰ (in. ³)(lb. ⁻²)	
Ti-8AC-1Mo-IV	138	149	15	0.05	300	Room Temp	2.25	30.0	1.125	1.06/1.05	1.48/1.49	
Ditto	138	149	15	0.05	300	Ditto	3.40	25.0	2.568	1.08/1.06	1.38/1.41	
Ditto	138	149	15	0.05	300	Ditto	4.20	19.0	3.920	1.06/1.05	1 98/2.0	
Ditto	:38	149	15	0.05	300	Ditto	8.0	11.3	14.220	1.07/1.06	291/294	
Ditto	138	149	15	0.05	300	Ditto	9.2	10	18.800	1.07/1.06	3.23/3.26	
Ditto	138	149	33.3	0.03	1100	Ditto	2.6	30	0.30	1.02/1.02	1.33/1.33	
Ditto	138	149	33.3	0.03	1100	Ditto	5.5	15	1.36	1.02/1.02	2.54/2.54	
Dιπο	138	149	70	0.03	2325	Ditto	4.25	30	0.18	1.05/1.04	0.79/8.0	
Ditto	138	149	70	0.03	2325	Ditto	9.20	15	0.86	1/1	1 53	

TABLE

Data summary for A	Inderson and S	Sullivan	for titan	ium-allo	y ressels						
Material properties			Vessel	geometr	y	Test condit	ions		Calculated valu	æ(*)	
Designation	σ _γ , ksi	σ _U , ksi	R, in.	t, in.	R/t	Temp, C	c, in	σů, ksi	50(c ² /R ²) tanh (R/50r)	φ,	(σ _N ² πcφ ₃) ⁻¹ 10 - 10 (in. ³)(lb. ⁻²)
Ti-5Al-2.5 Sn	193	220	3.0	0.02	150	- 196	0.06	190.4	0.02	x/1.76	0/0.83
Ditto	193	220	3.0	0.02	150	- 196	0.12	164.9	0.08	1.90/1.49	0.51/0.65
Ditto	193	220	3.0	0.02	150	- 196	11.0	156.6	0.06	1.63/1.38	0.72/0.85
Ditto	193	220	3.0	0.02	150	196	0.22	115.5	0.26	1.32/1.14	0.82/0.95
Ditto	193	220	3.0	0.02	150	- 196	0.23	105.1	0.29	1.26/1.18	0.99/1.06
Ditto	193	220	3.0	0.02	150	- 196	0.37	84.9	0.75	1.25/1.18	0.95/1.01
Ditto	193	220	3.0	0.02	150	- 196	0.38	74.6	0.80	1.18/1.13	1.27/1.33
Ditto	193	220	3.0	0.02	150	- 1 96	0.47	71.8	1.22	1.24/1.16	1.05/1.13
Ditto	193	220	3.0	0.02	150	- 196	0.49	66.2	1.33	1.21/1.14	1.22/1.30
Ditto	193	220	3.0	0.02	150	- 196	0.74	44.1	3.00	1.16/1.11	1.90/1.99
Ditto	193	220	3.0	0.02	150	196	0.73	35.9	2.90	1.09/1.07	3.10/3.16
Ditto	219	240	3.0	0.02	150	253	0.04	171.5	0.01	1.46/1.34	1.61/1.75
Ditto	219	240	3.0	0.02	150	- 253	0.07	160.9	0.03	1.39/1.30	1.14/1.22
Ditto	219	240	3.0	0.02	150	- 253	0.09	133.9	0.05	1.23/1.18	1.51/1.58
Ditto	219	240	3.0	0.02	150	- 253	0.13	121.4	0.10	1.20/1.16	1.30/1.34
Ditto	219	24	3.0	0.02	150	- 253	0.14	114.2	0.10	1.16/1.13	1.50/1.54
Ditto	219	240	3.0	0.02	150	-253	0.26	84.6	0.37	1.11/1.09	1.54/1.56
Ditto	219	240	3.0	0.02	150	- 253	0.24	76 0	0.32	1.08/1.06	2.12/2.15
Ditto	219	240	3.0	0.02	150	- 253	0.40	63.6	0.88	1.09/1.08	1.79/1.82
Ditto	219	240	3.0	0.02	150	253	0.47	63.0	1.22	1 13/1.09	1.52/1.55
Ditto	219	240	3.0	0.02	150	- 253	0.38	61.5	0.80	1.08/1.07	2.05/2.06
Ditto	219	240	30	0.02	150	-253	0.49	51.6	1.33	1.08/1.06	2.25/2.30
Ditto	219	240	3.0	0.02	150	- 253	0.80	40.6	3.55	1.11/1.09	2.17/2.21
Ditto	219	240	3.0	0.02	150	- 253	0.78	37.7	3.38	1.08/1.07	2.65/2.68

^(a) Two values are computed for φ_3 and $\sigma_H^{*2}\pi c \varphi_3$ corresponding to the upper and lower bounds for $\tilde{\sigma}: \tilde{\sigma} = \sigma_{\tilde{\tau}}, \tilde{\sigma} = \sigma_{\tilde{v}}$.

[&]quot;The R=15-in. tests involved cylindrical vessels, the R=33.3-ia. and 70-in. tests involved curved panels.

"Two values are computed for φ_3 and $\sigma_R^{12}\pi c \varphi_3$ corresponding to the upper and lower bounds for $\hat{\sigma}: \hat{\sigma} = \sigma_g$, $\hat{\sigma} = \sigma_g$.

TABLE

Data summary for Sechler and Williams for brass vessels

Material propertie	\$		Vessel	g c omet ry	,	Test condition	75		Calculated valu		
Designation .	σ _y , ksi	σ _υ , ksi	R, in.	f, in.	R,I	Temp, C	<i>c</i> , in.	σ _H , ksı	50(c ² R ²) tanh (R.50r)		$(\sigma_H^{*2}\pi c \varphi_3)^{-1}$ 10 ⁻¹⁰ (in. ³)(lb. ⁻²)
Brass ^(b)	45	57	1.5	0.001	1500	Room Temp	0.03	50.6	0.02	x/1.86	0/22.3
Ditto	45	57	1.5	0.001	1500	Ditto	0.04	45.4	0.03	∞/1.52	0/25.4
Ditto	45	57	1.5	0.001	1500	Ditto	0.06	37.1	0.08	1.74/1.71	22.18/29.47
Ditto	45	57	1.5	0.001	1500	Ditto	0.10	30.0	0 22	1'44:1.21	24.53/29.2
Ditto	45	57	1.5	100.0	1500	Ditto	0.10	30.0	0.22	1.44, 1.21	24.13/29.2
Ditto	45	57	1.5	0.001	1500	Ditto	0.12	25.5	0.32	1.31/1.16	31.15/35.18
Ditto	45	57	1.5	0.001	1500	Ditto	0.12	25.7	0.32	1.31/1.16	30.65/34.62
Ditto	45.	57	1.5	100.0	1500	Ditto	0.13	26.8	0.37	1.39/1.19	24.55 24.68
Ditto	45	57	1.5	0.001	1500	Ditto	0.15	24.0	0.50	1.33/1.17	27.74/31.53
Ditto	45	57	1.5	0.001	1500	Ditto	0.15	21.7	0.50	1.25/1.13	36.03 39.86
Ditto	45	57	1.5	0.001	1500	Ditto	0.17	19.1	0.64	1.20; 1.11	42.73/46.2
Ditto	45	57	1.5	0.001	1500	Ditto	0.21	19.1	0.98	1.28/1 15	32.55, 36 23
Ditto	45	57	1.5	0.001	1500	Ditto	0.25	14.2	1.38	1.17:1.10	54 09/57.53
Ditto	45	57	1.5	0.001	1500	Ditto	0.30	13.3	2.00	1.21/1.11	49.48-53.94
Ditto	45	57	1.5	0.001	1500	Ditto	0 35	11.0	2.70	1.16/1.09	64.81.68.97
Ditto	40	53.7	2.5	0.001	2500	Ditto	0.032	48.0	0.008	x/1.86	0.23.17
Ditto	40	53.7	2.5	0.001	2500	Ditto	0.032	46.1	0.008	x/1.66	0 28 14
Ditto	40	5: 7	2.5	0.001	2500	Ditto	0 062	40 0	0.03	x/1.40	0 22 89
Ditto	40	53.7	2.5	0.001	2500	Ditto	0.094	37.0	0.07	2.6 , 1.36	9.52 18.2
Ditto	40	53.7	2.5	0.001	2500	Ditto	0.094	38 7	0.07	x/1.46	0 16 16
Ditto	40	53.7	2.5	0.001	2500	Ditto	0.10	35.0	86.0	1.98, 1.30	13.11 19.98
Ditto	40	53.7	2.5	0 001	2500	Ditto	0 125	32.2	0.12	1.76 1.26	13 96 19:50
Ditto	40	53.7	2.5	100.0	2500	Ditto	0.125	30.2	0.12	1.54, 1.21	18.13 13.08
Ditto	40	53.7	2.5	0.001	2500	Ditto	0.15	27.5	0.18	1.44.1.18	19.50 21 80
Ditto	40	53.7	2.5	0.001	2500	Ditto	0 156	26.2	0.20	1.39.1 16	21 41 25 65
Ditto	40	53.7	2.5	0.001	2500	Ditto	0.156	27.0	0.20	1.43 1.18	19.58 23.73
Ditto	52	63.2	2.5	0 003	833	Ditto	0.048	56.4	0018	x/186	0 11 2
Ditto	52	63.2	2.5	0.003	833	Ditto	0.098	50.0	0.076	\$,1.60	0 811
Ditto	52	63 2	2.5	0.003	833	Ditto	0115	48.4	0.10	x /1 54	0 167
Ditto	52	63.2	2.5	0.003	833	Dato	0.125	42.5	0.12	x, 1 54	0.915
Ditto	52	63.2	2.5	0.003	833	Ditto	0.125	45.0	012	2.24 1.44	5.61 877
Ditto	52	63.2	2.5	0.003	833	Ditto	0.125	43.2	0.12	1 88 1 22	8 25 11 18
Ditto	52	63.2	2.5	0.003	833	Ditto	0.148	413	0.1	1.85 1.38	810. 913

Two values are computed for φ₃ and σ_H² πεφ₃ corresponding to the upper and lower bounds for ĉ. ĉ = c₁, ĉ = c₁.
 Brass shim stock.

